Model Building in Phenix

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The Crystallographic Process



The Crystallographic Model

- Atoms (spherical or ellipsoid)
- Mean square displacements (B-factors)
- Occupancy
- Chemical restraints (e.g. bond lengths, angles, etc)









Electron Density Maps

Real and reciprocal spaces are related by Fourier
Transformation



• Experimental phasing

$$m_{obs}F_{obs}e^{i\phi_{obs}}$$

$$m_{dm}F_{obs_{dm}}e^{i\phi_{dm}}$$

[Any missing Fobs generated from density modification]

Molecular Replacement

$$m_{dm}F_{obs_{dm}}e^{i\phi_{dm}}$$

[Any missing Fobs generated from density modification]







Effect of Errors in Atomic Position

- Atomic errors give "boomerang" distribution of possible atomic contributions
- Portion of atomic contribution is correct



Structure factor with coordinate errors

- Same direction as the sum of the atomic f
 - but shorter by 0< D < I
 - D=f(resolution)
- Central Limit Theorem
 - Many small atoms
 - Gaussian distribution for the total summed F
 - $\sigma_{\Delta} = f(resolution)$









Estimated Error in Maps - σ_A

• When an atomic model is available, estimates of errors arising from the model can be made.



 $|\Delta \mathbf{F}|^2 = |\mathbf{F}_{\mathcal{O}}|^2 + D^2 |\mathbf{F}_{\mathcal{O}}|^2 - 2D|\mathbf{F}_{\mathcal{O}}|\mathbf{F}_{\mathcal{O}}|\cos(\Delta\alpha)$ $\mathbf{F}_{O} \approx (2m|\mathbf{F}_{O}| - D|\mathbf{F}_{C}|) \exp(i\alpha_{C})$ $(2m|\mathbf{F}_{\mathcal{O}}| - D|\mathbf{F}_{\mathcal{C}}|) \exp(i\alpha_{\mathcal{C}})$ Model phased map + Difference map $(m|\mathbf{F}_{O}| - D|\mathbf{F}_{C}|) \exp(i\alpha_{C})$ Difference map $m_{comb} 2F_{obs} e^{i\phi_{comb}} - D_{\sigma} F_{calc} e^{i\phi_{calc}}$ $m_{comb}F_{obs}e^{i\phi_{comb}} - D_{\sigma}F_{calc}e^{i\phi_{calc}}$ [Difference map] $m_{\sigma} 2F_{obs}e^{i\phi_{calc}} - D_{\sigma}F_{calc}e^{i\phi_{calc}}$

$$m_{\sigma_A}F_{obs}e^{i\phi_{calc}} - D_{\sigma_A}F_{calc}e^{i\phi_{calc}}$$

[Difference map]







High Resolution Maps





- High resolution maps (1.5Å or better) are typically easy to interpret, although time consuming)
- Biggest challenge is recognizing and modelling discrete disorder and atomic motion



Image from Phil Evans, LMB MRC Cambridge





Low Resolution Maps



- Low resolution maps (3.5Å and worse) are typically very difficult to interpret.
- The lack of detail makes it difficult to determine the identity of residues.
- At very low resolution the use of similar structural motifs can greatly aide the process





Image from Phil Evans, LMB MRC Cambridge



Divide-and-Conquer



- Manual model building typically requires that the map interpretation be divided up into different stages:
 - Tracing the polymer backbone then adding the chemical identities for the polymer units (e.g. amino acids)







Automated Model Building

- The process of map interpretation can also be performed computationally.
 - Is less time consuming for the user
 - Object decision-making can minimize errors
- Automated methods typically rely on some kind of pattern matching algorithm to extract information from the map.







Map Interpretation with Larger Fragments

- RESOLVE uses pattern matching methods to automate the model building process:
 - FFT-based identification of helices and strands
 - Extension with tri-peptide libraries
 - Probabilistic sequence alignment
 - Automatic molecular assembly
- RESOLVE uses larger fragments than individual atoms so is able to perform well even at medium to low resolution







Locating Fragments



- Fragments:
 - Helical template: 6 amino acids, average density from ~200 6-amino acid helical segments
 - Helix fragment library: 53 helices 6-24 amino acid long
 - Beta-sheet template: 4 amino acid, average density
 - Beta-sheet fragment library: 24 strands 4-9 amino acid long
- Identify possible template locations with FFT-based convolution search
- Maximize correlation coefficient of template with map
- Superimpose each fragment in corresponding library (helix, sheet) on template
- Identify longest segment in good density, score = <density>*sqrt(Natoms)







Fragment Extension



- Tri-peptide fragment library
 - N-terminal extension (3 full amino acids), 9232 members
 - C-terminal extension (CA C O + 2 full amino acids), 4869 members
- Look-ahead scoring: find fragment that can itself be optimally extended
- Each of 10000 fragments: superimpose CA C O on same atoms of last residue in chain (extending by 2 residues): pick best 10
- Each of best 10: extend again by 2 residues and pick best 1:









The Final Mainchain Trace



- Choose highest-scoring fragment
- Test all overlapping fragments as possible extensions
- Choose one that maximizes score when put together with current fragment
- When current fragment cannot be extended: remove all overlapping fragments, choose best remaining one, and repeat







Assigning the Sequence

• The sequence is assigned to the mainchain by a probabilistic alignment method, determining the relative probability of every amino acid at each position (based on density and sequence composition)

#	G	A	s	v	Т	L	м	С	F	Y	к	R	w	н	E	D	Q	N	Р	т
1	6	5	4	18	18	6	1	1	1	2	6	2	2	1	9	6	1	0	1	4
2	4	11	14	37	5	2	0	2	0	0	2	3	0	٥	1	2	0	0	0	6
3	11	23	5	12	5	3	2	0	1	3	7	3	1	٥	5	3	2	0	2	2
4	7	9	6	16	8	5	2	0	1	3	8	4	1	0	7	6	2	0	3	4
5	31	7	3	7	4	2	1	0	1	3	5	4	1	0	6	2	2	0	11	1
6	1	3	3	41	14	8	0	0	0	0	2	1	0	٥	2	4	0	0	1	9
7	0	0	o	O	O	0	o	0	15	63	1	o	17	1	D	0	0	0	0	o
8	2	3	6	23	10	6	2	1	0	1	4	3	0	0	5	16	1	0	1	6
9	96	0	0	0	O	0	o	0	0	0	o	o	o	o	D	0	0	0	0	o







Side Chain Addition



- Best rotamers, based on correlation coefficient are used
- Refinement is required







Rapid Secondary Structure Fitting

- Secondary structure elements have recognizable features, even at low resolution (e.g. α-helices look like tubes)
- The essential features (e.g. the long axis of the α-helix) can often be identified
- Once identified, the density can be analyzed further to determine position and orientation











Rapid Secondary Structure Fitting

- The distribution of density at the main chain atomic positions and the sidechains can be used to determine direction and derive accurate C_{α} positions
- This is very quick (seconds to minutes)
- Can be followed by sidechain fitting to create a fairly complete model
- Similar methods can be applied to find β-sheets





High Resolution Data is Not Required



Calcium release channel 3.1 Å. Data courtesy of P. Nissen

- This rapid method works even at modest resolution
- Can be used to determine if structure solution is likely given the current experimental phases
- Success will depend on the quality of the phases (more than the resolution)







Nucleic Acid Model Building



Group II intron at 3.5 Å. Data courtesy of J. Doudna

- Nucleic acid structures can be built using fragment location (short A-form or B-form helices), followed by extension
- Works well even with low resolution
- Current limitation is the simultaneous building of protein and nucleic acid







Automated Model Building/Rebuilding







Automated Building Depends on Data Quality



- Automated model building results are relatively independent of resolution
- Results are more dependent on data quality and intrinsic quality of the electron density map





Tom Terwilliger, Los Alamos National Laboratory



Automated Model Building for Cryo-EM

- Higher resolution (4.5Å and better) makes automated building possible
- Being developed in Phenix by Tom Terwilliger (Los Alamos National Lab):
 - Automatically segmenting maps and extracting the asymmetric unit of reconstruction
 - Create maps that emphasize information at various resolutions by variable map sharpening
 - Trace the protein main chain using nearly-constant $C_{\alpha}\text{-}C_{\alpha}\text{-}C_{\alpha}$ distances and angles
 - Identify direction of the main-chain in models by fit to density







Automated Model Building



Automated segmentation of emd_6224 (anthrax toxin protective antigen pore at 2.9 Å; Jiang *et al.* 2015)

Tom Terwilliger (LANL), Oleg Sobolev (LBNL)





Automated Model Building



Cryo-EM map from the yeast mitochondrial ribosome (chain I of large subunit, 3.2Å, Amunts et al., 2014)

Autobuilt model (pink) Deposited model (green)

(only main-chain and C_{β} atoms shown)

Tom Terwilliger (LANL), Oleg Sobolev and Pavel Afonine (LBNL)







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