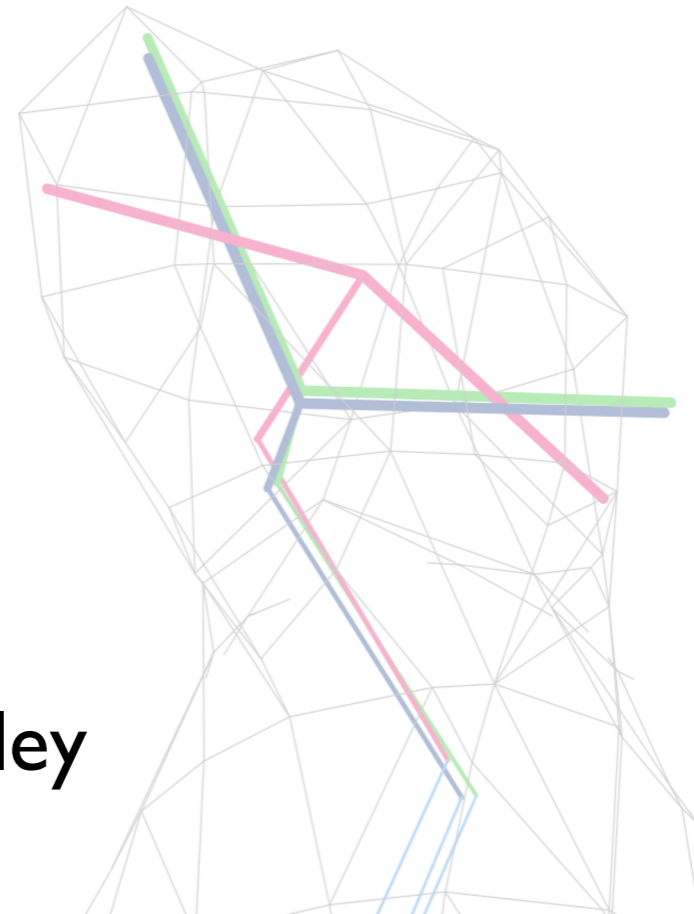
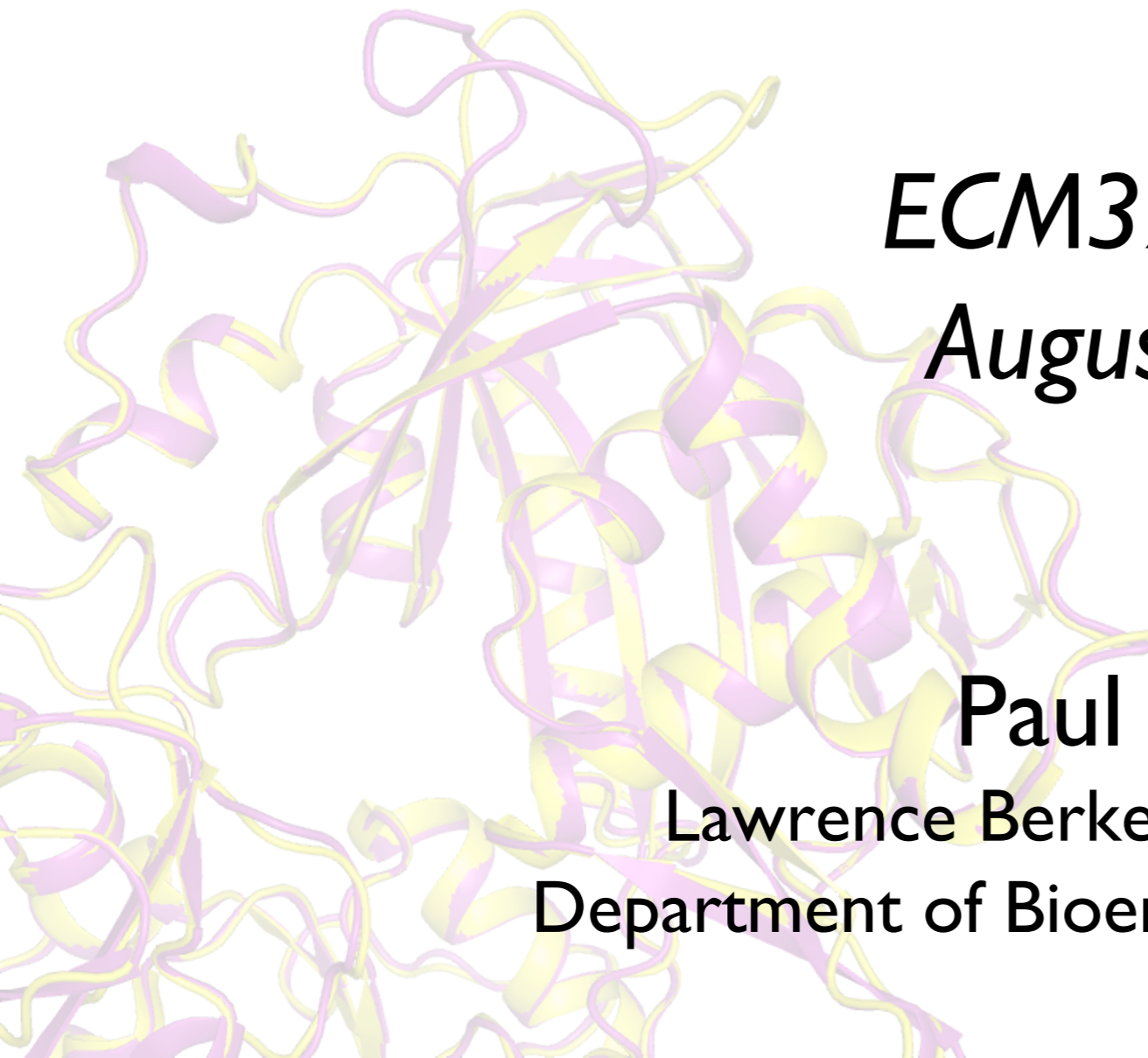


# Model Validation at Low Resolution

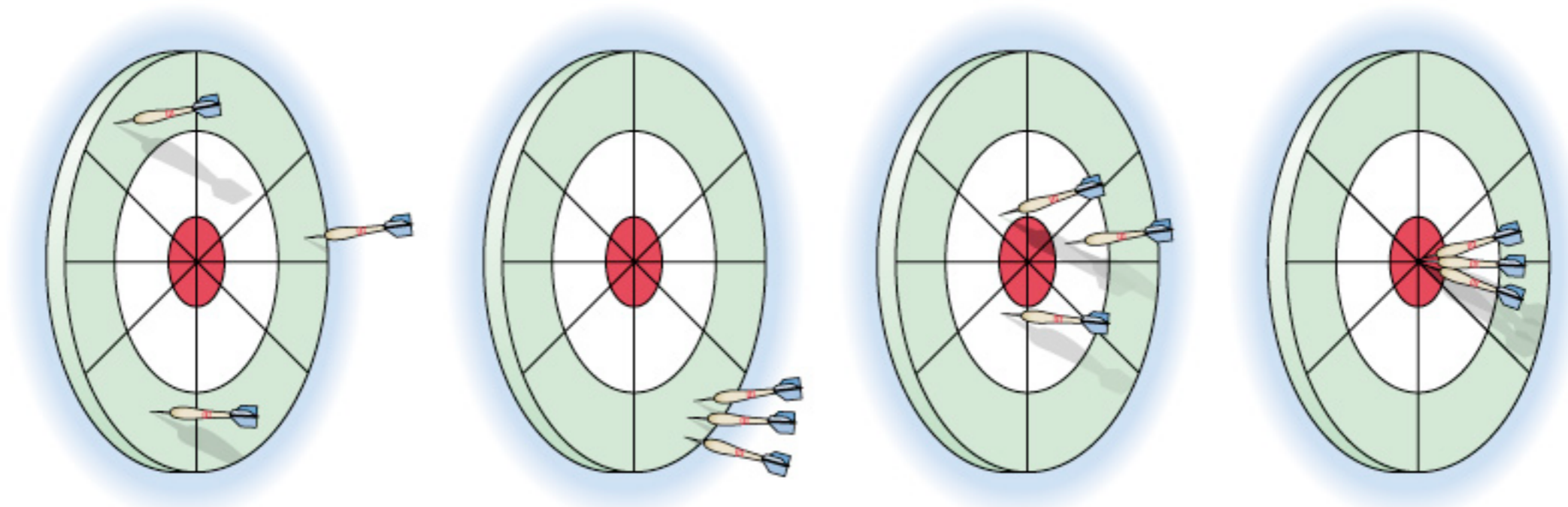
*ECM32 Vienna  
August 2019*

**Paul Adams**

Lawrence Berkeley Laboratory and  
Department of Bioengineering UC Berkeley



# Accuracy & Precision



**(a)** Low accuracy  
Low precision

**(b)** Low accuracy  
High precision

**(c)** High accuracy  
Low precision

**(d)** High accuracy  
High precision

From <http://extensionengine.com>, by Furqan Nazeeri

# Errors

- Random errors (noise)
  - Typically normally distributed
  - Can be reduced by increasing the number of observations
  - Affect the precision
- Systematic errors (bias)
  - Could arise from a poor experimental design or lack of understanding of the system being studied
  - Are reproducibly biased
  - Affect the accuracy
- Gross errors
  - Incorrect assumptions have been made or serious mistakes undetected
  - May be detectable as outliers compared to prior knowledge

# Mistakes Still Happen

## Retraction

WE WISH TO RETRACT OUR RESEARCH ARTICLE "STRUCTURE OF MsbA from *E. coli*: A homolog of the multidrug resistance ATP binding cassette (ABC) transporters" and both of our Reports "Structure of the ABC transporter MsbA in complex with ADP•vanadate and lipopolysaccharide" and "X-ray structure of the EmrE multidrug transporter in complex with a substrate" (1–3).

The recently reported structure of Sav1866 (4) indicated that our MsbA structures (1, 2, 5) were incorrect in both the hand of the structure and the topology. Thus, our biological interpretations based on these inverted models for MsbA are invalid.

An in-house data reduction program introduced a change in sign for anomalous differences. This program, which was not part of a conventional data processing package, converted the anomalous pairs (I+ and I-) to (F- and F+), thereby introducing a sign change. As the diffraction data collected for each set of MsbA crystals and for the EmrE crystals were processed with the same program, the structures reported in (1–3, 5, 6) had the wrong hand.

The error in the topology of the original MsbA structure was a consequence of the low resolution of the data as well as breaks in the elec-

tron density for the connecting loop regions. Unfortunately, the use of the multicopy refinement procedure still allowed us to obtain reasonable refinement values for the wrong structures.

The Protein Data Bank (PDB) files 1JSQ, 1PF4, and 1Z2R for MsbA and 1S7B and 2F2M for EmrE have been moved to the archive of obsolete PDB entries. The MsbA and EmrE structures will be recalculated from the original data using the proper sign for the anomalous differences, and the new C $\alpha$  coordinates and structure factors will be deposited.

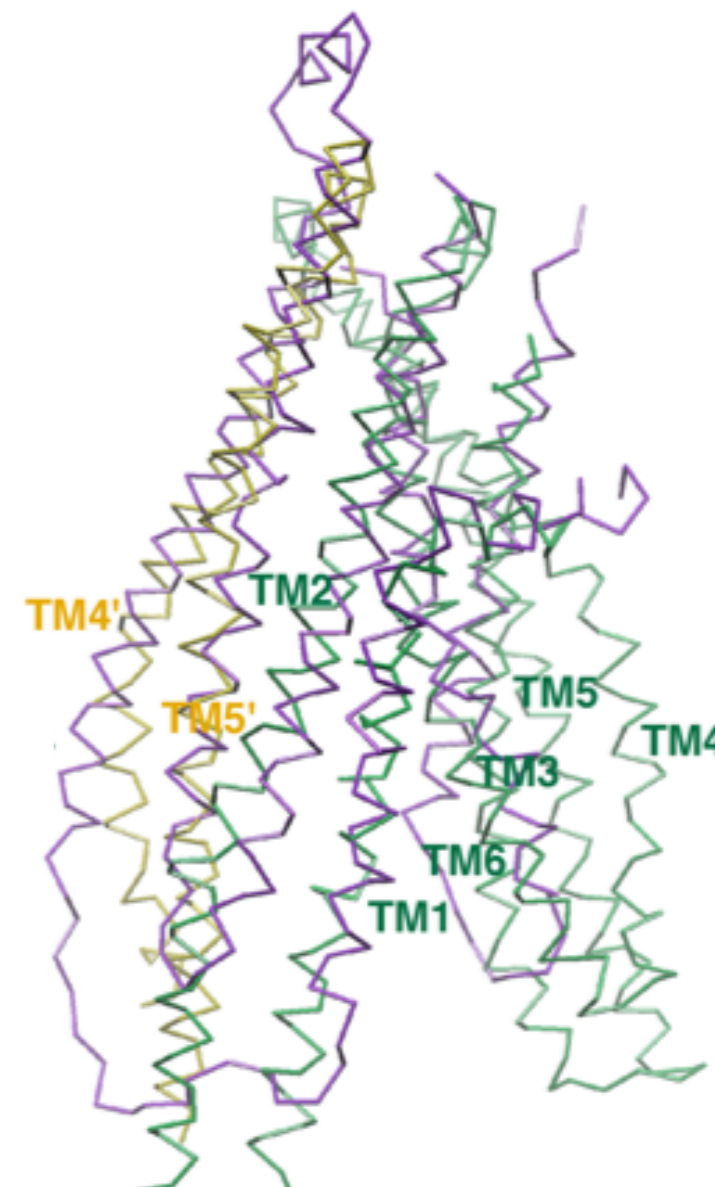
We very sincerely regret the confusion that these papers have caused and, in particular, subsequent research efforts that were unproductive as a result of our original findings.

GEOFFREY CHANG, CHRISTOPHER B. ROTH,  
CHRISTOPHER L. REYES, OWEN PORNILLOS,  
YEN-JU CHEN, ANDY P. CHEN

Department of Molecular Biology, The Scripps Research Institute, La Jolla, CA 92037, USA.

### References

1. G. Chang, C. B. Roth, *Science* **293**, 1793 (2001).
2. C. L. Reyes, G. Chang, *Science* **308**, 1028 (2005).
3. O. Pornillos, Y.-J. Chen, A. P. Chen, G. Chang, *Science* **310**, 1950 (2005).
4. R. J. Dawson, K. P. Locher, *Nature* **443**, 180 (2006).
5. G. Chang, *J. Mol. Biol.* **330**, 419 (2003).
6. C. Ma, G. Chang, *Proc. Natl. Acad. Sci. U.S.A.* **101**, 2852 (2004).



## Retraction: Cocrystal structure of synaptobrevin-II bound to botulinum neurotoxin type B at 2.0 Å resolution

Michael A Hanson & Raymond C Stevens

*Nat. Struct. Biol.* **7**, 687–692 (2000); retracted 6 July 2009

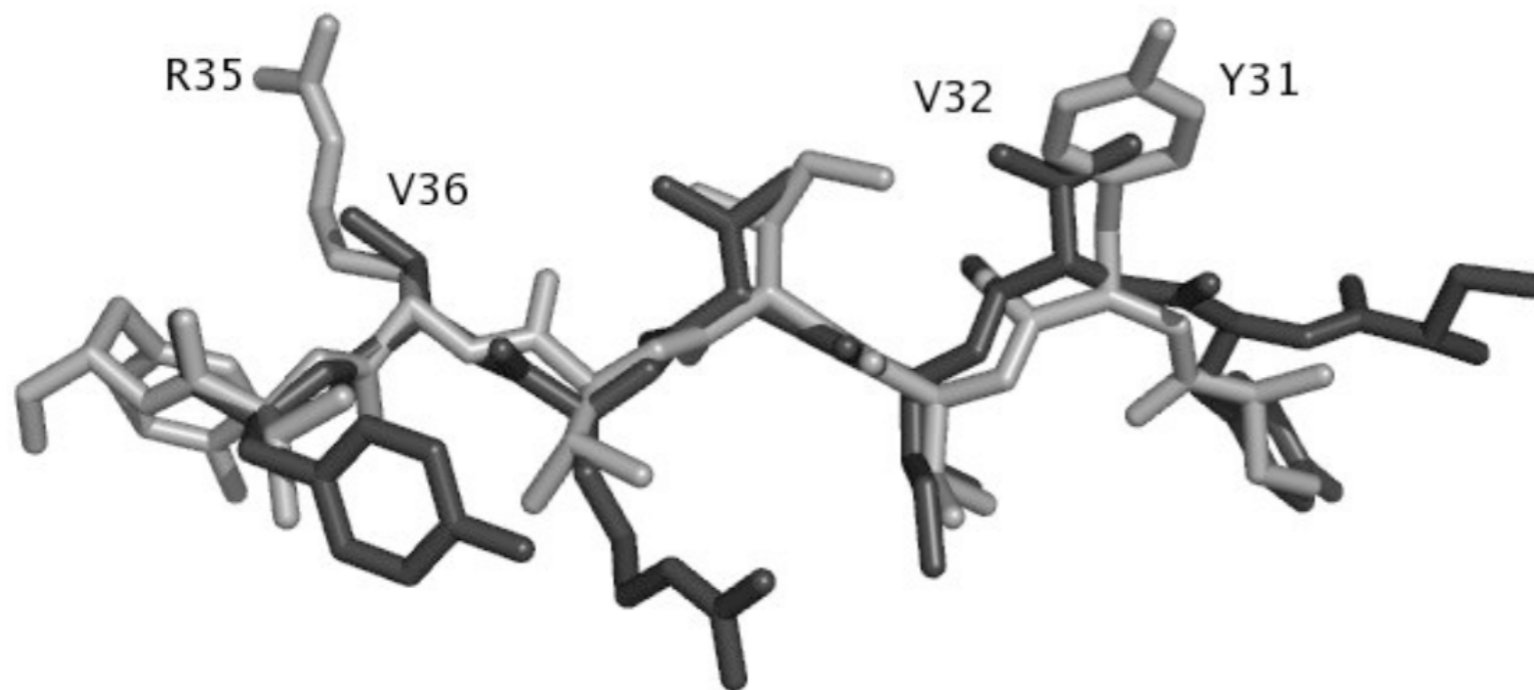
In this paper, we described both the three-dimensional crystal structure of a botulinum toxin catalytic domain separated from the holotoxin (BoNT/B-LC, PDB 1F82) and a structure of the toxin catalytic domain in complex with a peptide (Sb2–BoNT/B-LC, PDB 1F83). The complex was later refined and deposited in the Protein Data Bank (PDB 3G94). The apo structure (PDB 1F82) remains valid. However, because of the lack of clear and continuous electron density for the peptide in the complex structure, the paper is being retracted. We apologize for any confusion this may have caused.

Dawson & Locher, *Nature*  
**443**, 180–185, 2006



# Register Errors

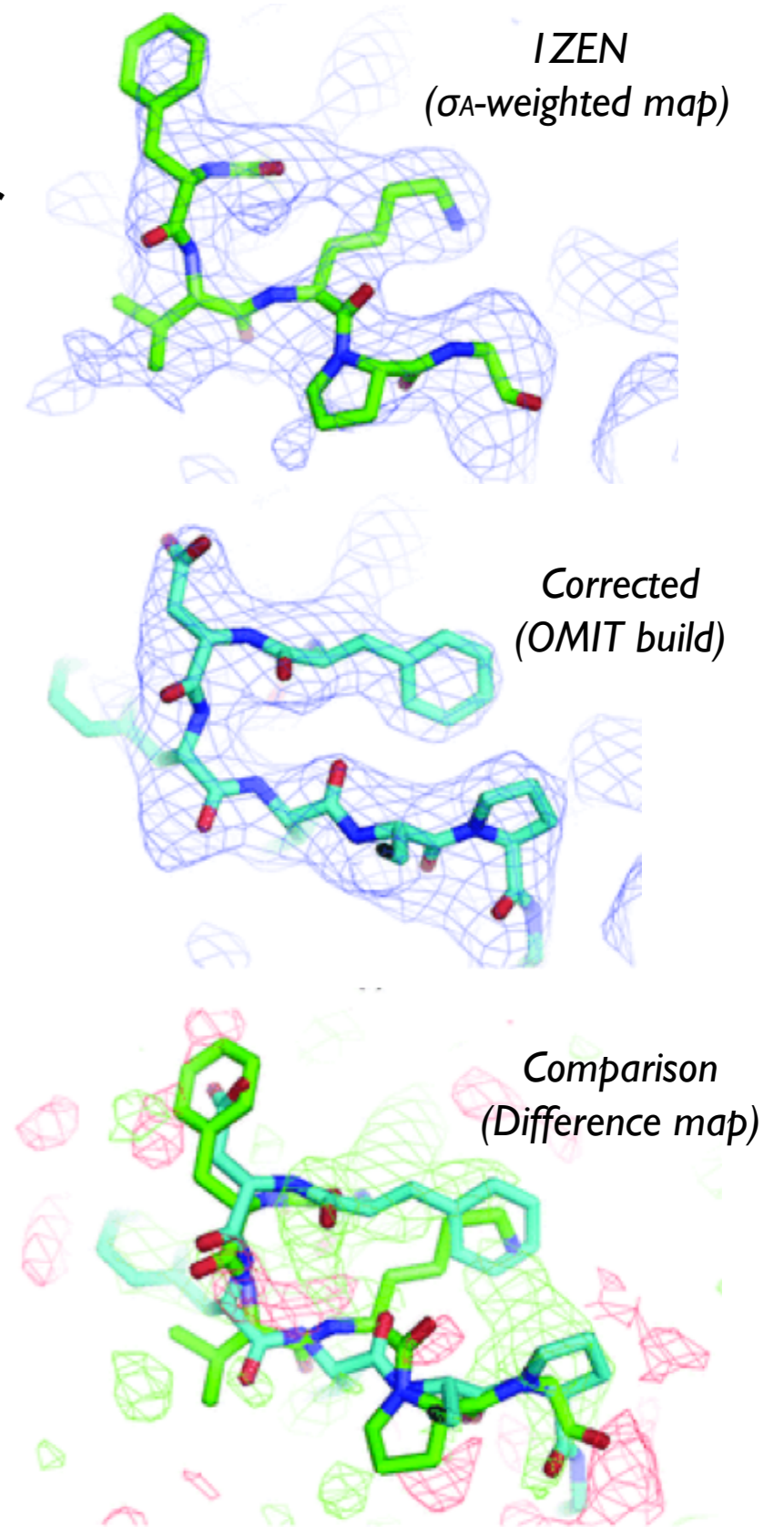
- Register errors typically start in loop regions (over or under building)
- Fixing these errors can be challenging (loop regions often have poor density) - estimated that 1% of structures in PDB have register errors
- Real space analysis can help
- Packing analysis (WHATCHECK, MolProbity)



*1CHR, 3.0 (light) versus 2CHR (dark)*

*Image from Gerard Kleywegt, European Bioinformatics Institute*

**Phenix**

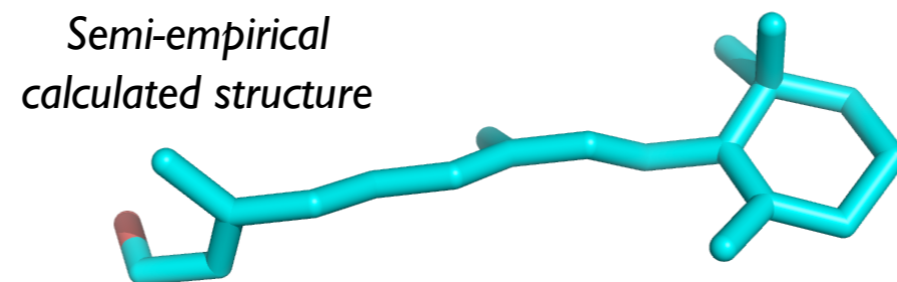
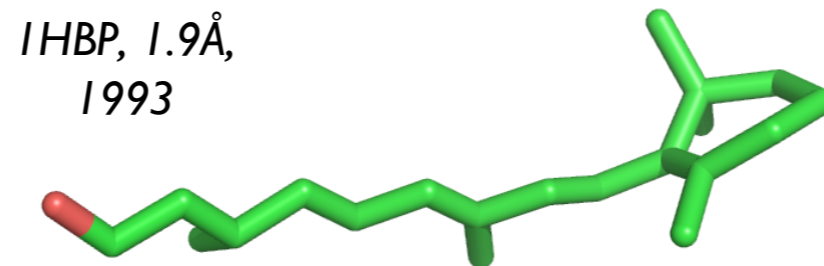


Terwilliger et al., *Acta Cryst*  
D64, 515-524, 2008



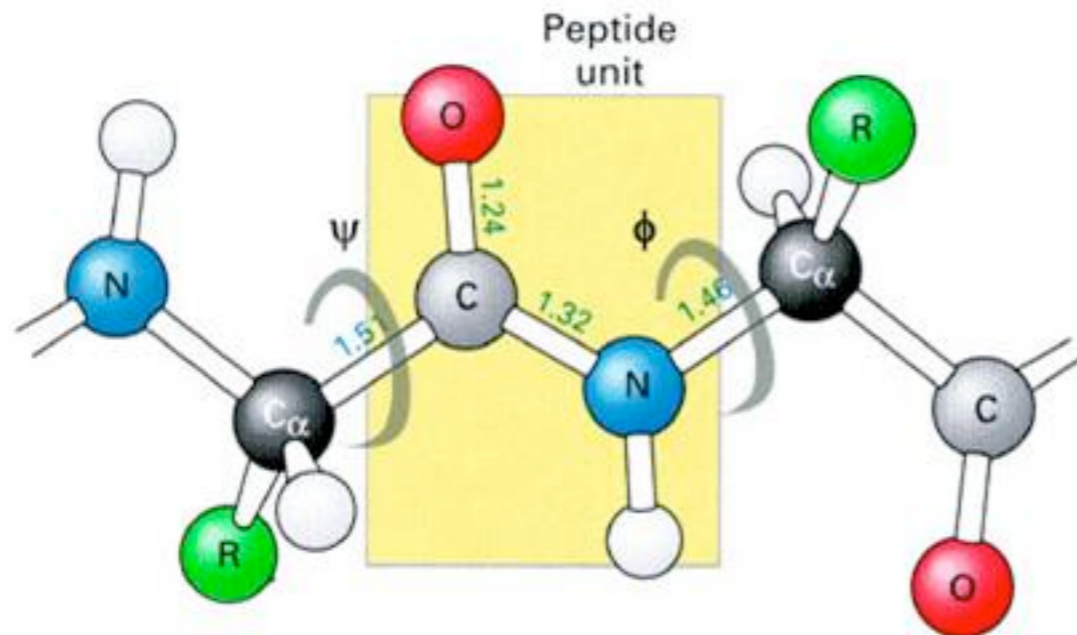
# Other Kinds of Errors

- Systematic error in magnification
- Incorrect sequence (less common these days)
- Incorrectly placed waters or too many waters
- Waters fit instead of ions and side chains
- Small molecule geometry (where did you get the restraints from?)



# Geometric Measures

- Some of the best measures for validation are from information not used in the model optimization (e.g. Free R-value)
- For geometry (of proteins) one of the best measures is the Ramachandran distribution - the main chain torsion angles
- The handedness of amino acids, and the steric clashes that occur, given the side chain attachment to the mainchain, results in limits on the distribution of mainchain torsion angles



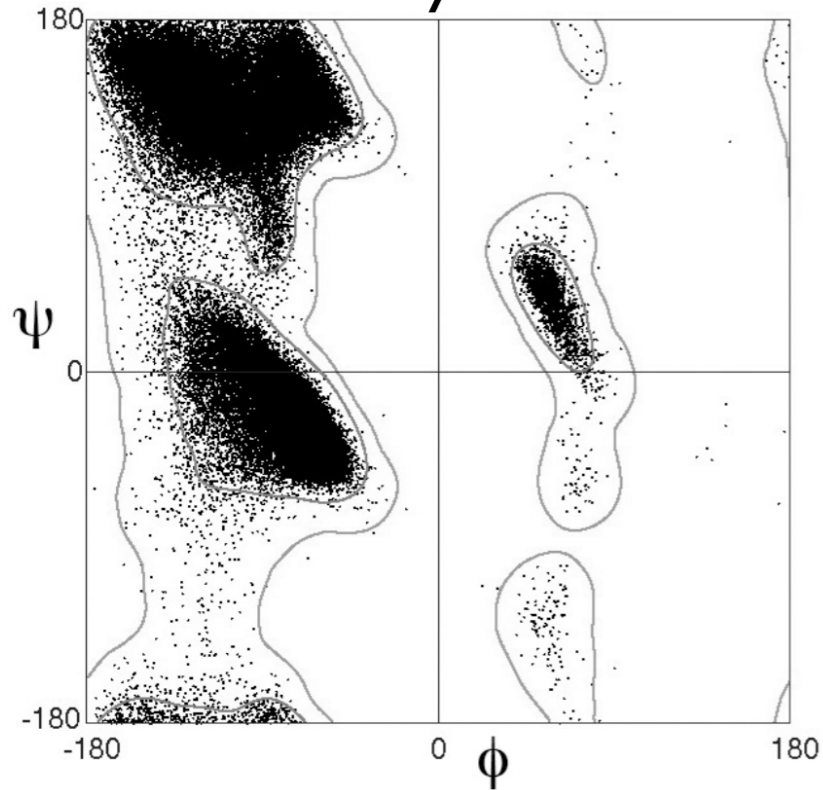
G. N. Ramachandran

**Phenix**

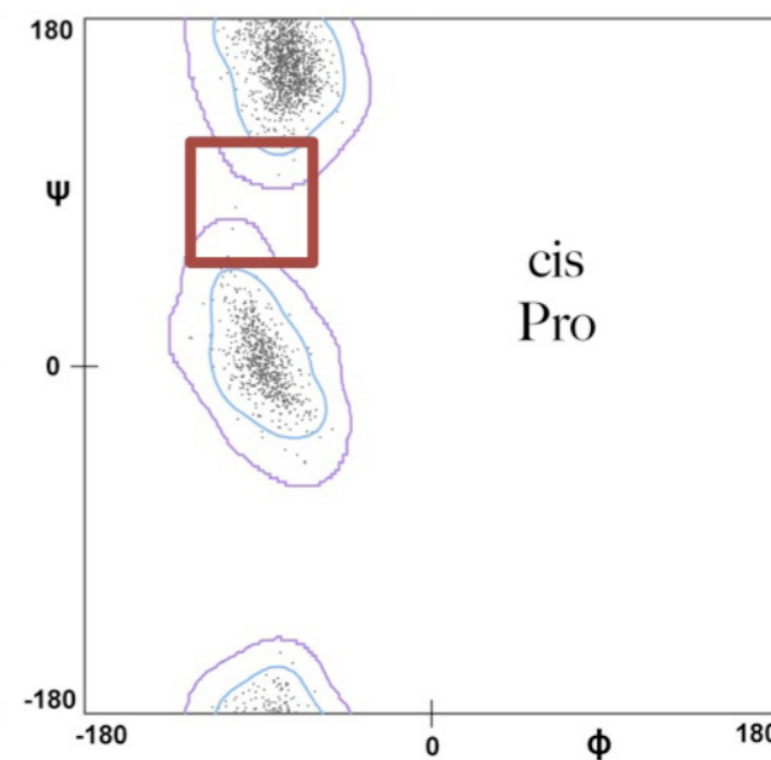
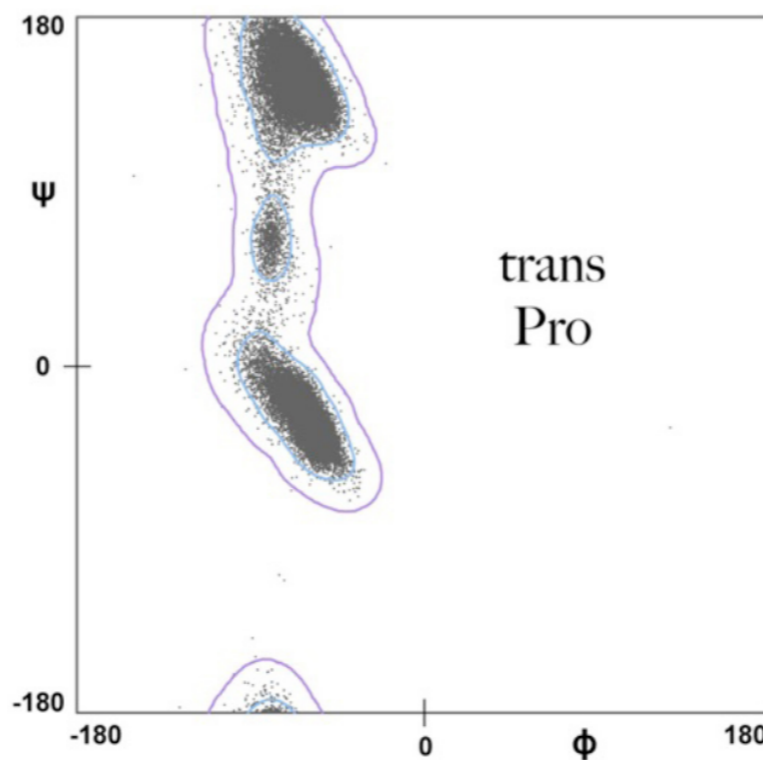
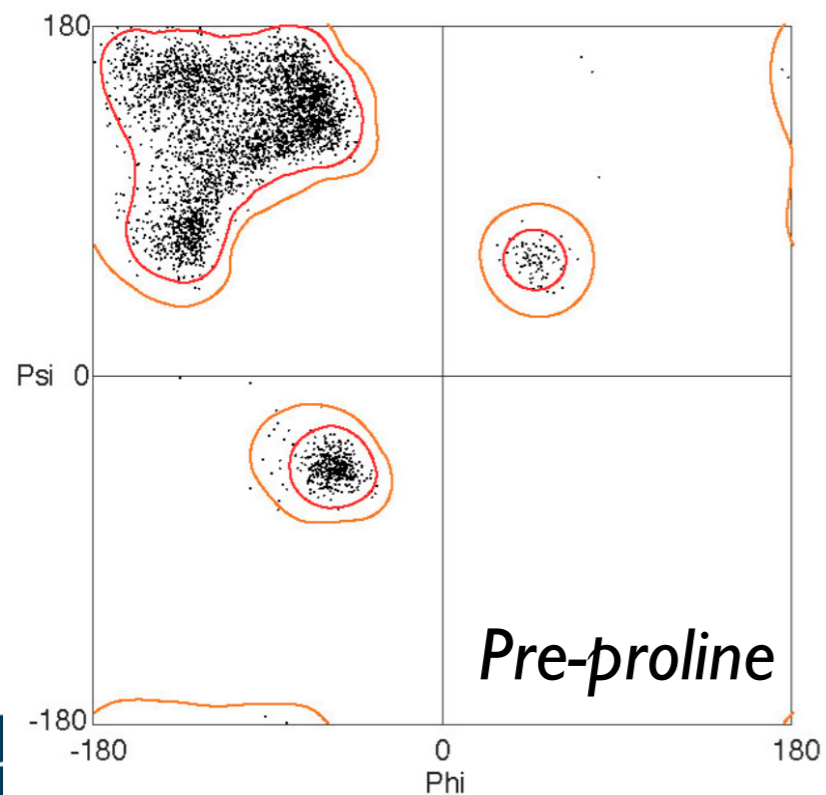
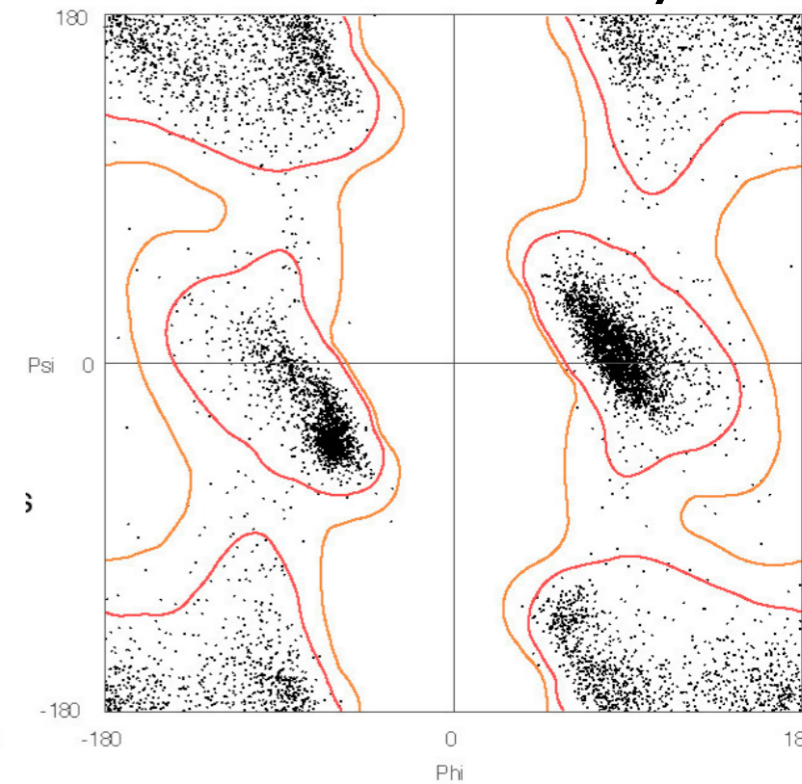
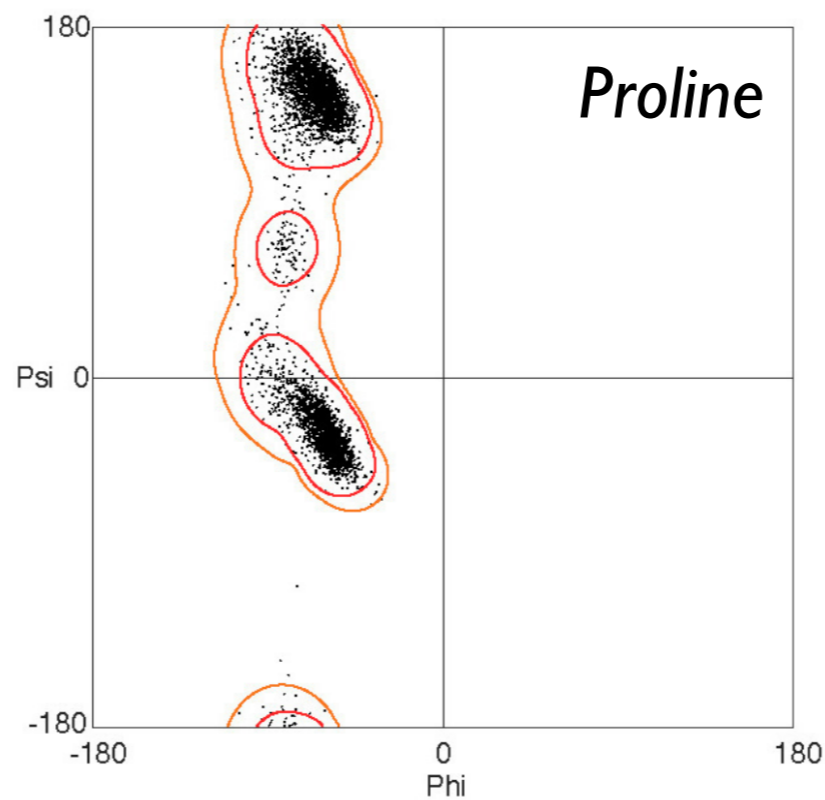


# The Ramachandran Plot

All minus  
Pro & Gly



Glycine

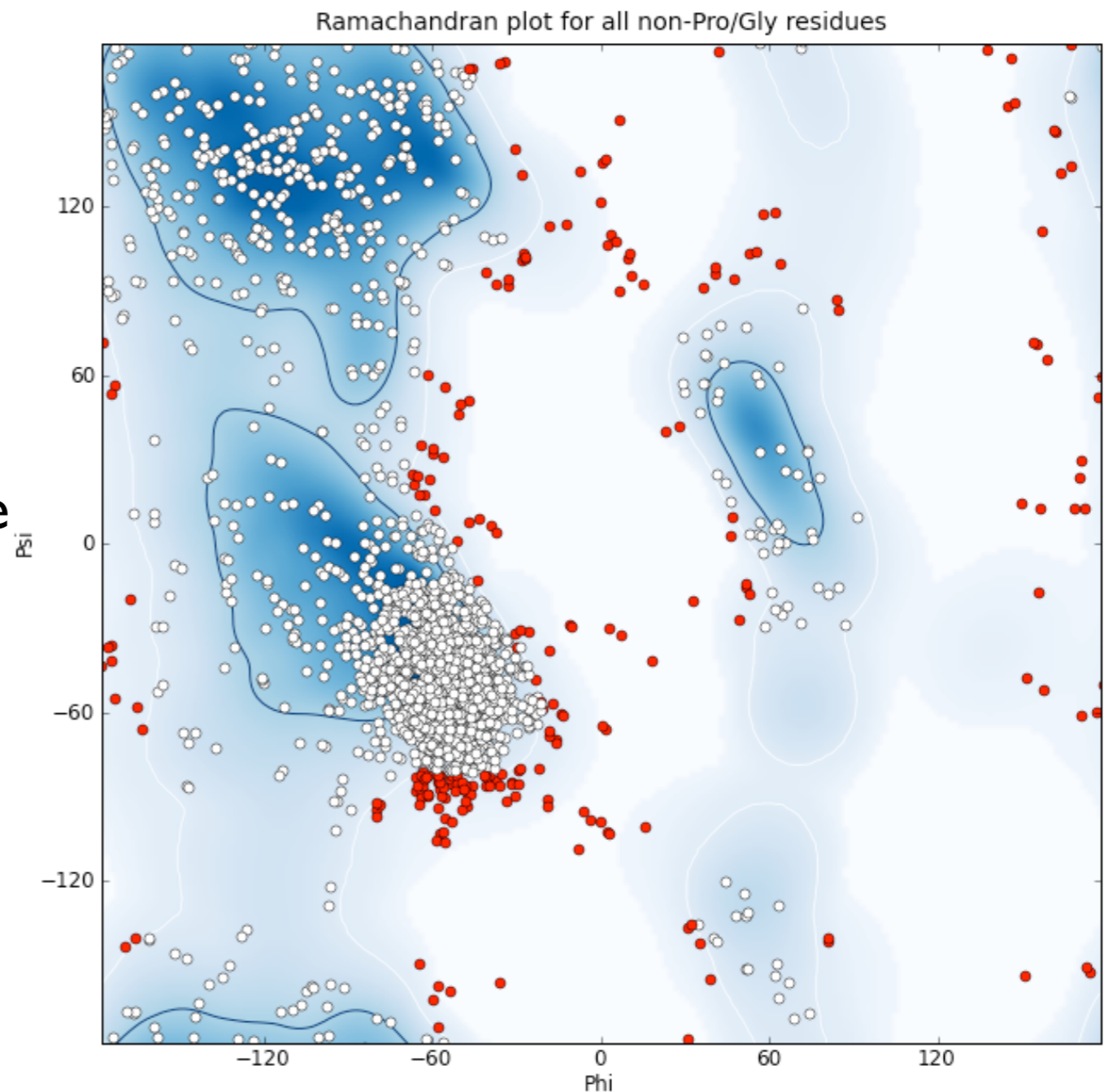


Images from Jane and David  
Richardson, Duke University



# The Ramachandran Plot

- A protein structure should in general conform to prior expectations (based on theory and prior observation)
- Most (98%+) residues should have a mainchain conformation consistent with the Ramachandran distribution
- A small percentage (0.2%) of residue may show Ramachandran outliers (note they are not necessarily errors)
  - Outliers can be seen in strained regions of the structure (e.g. in the active site)
- Any outliers need to be confirmed by detailed analysis



# Rotamers

- There are steric clashes between atoms within amino acid side chains
- These clashes lead to preferred conformations, called rotamers
- Different rotamers are generated by rotation of side chain torsion angles ( $\chi_1$ ,  $\chi_2$  etc)

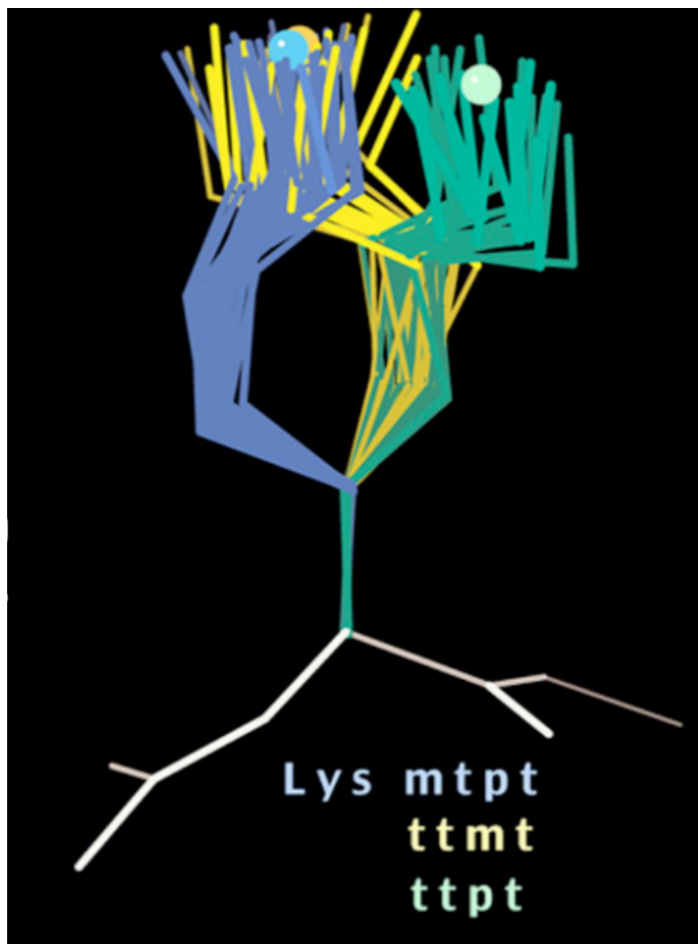
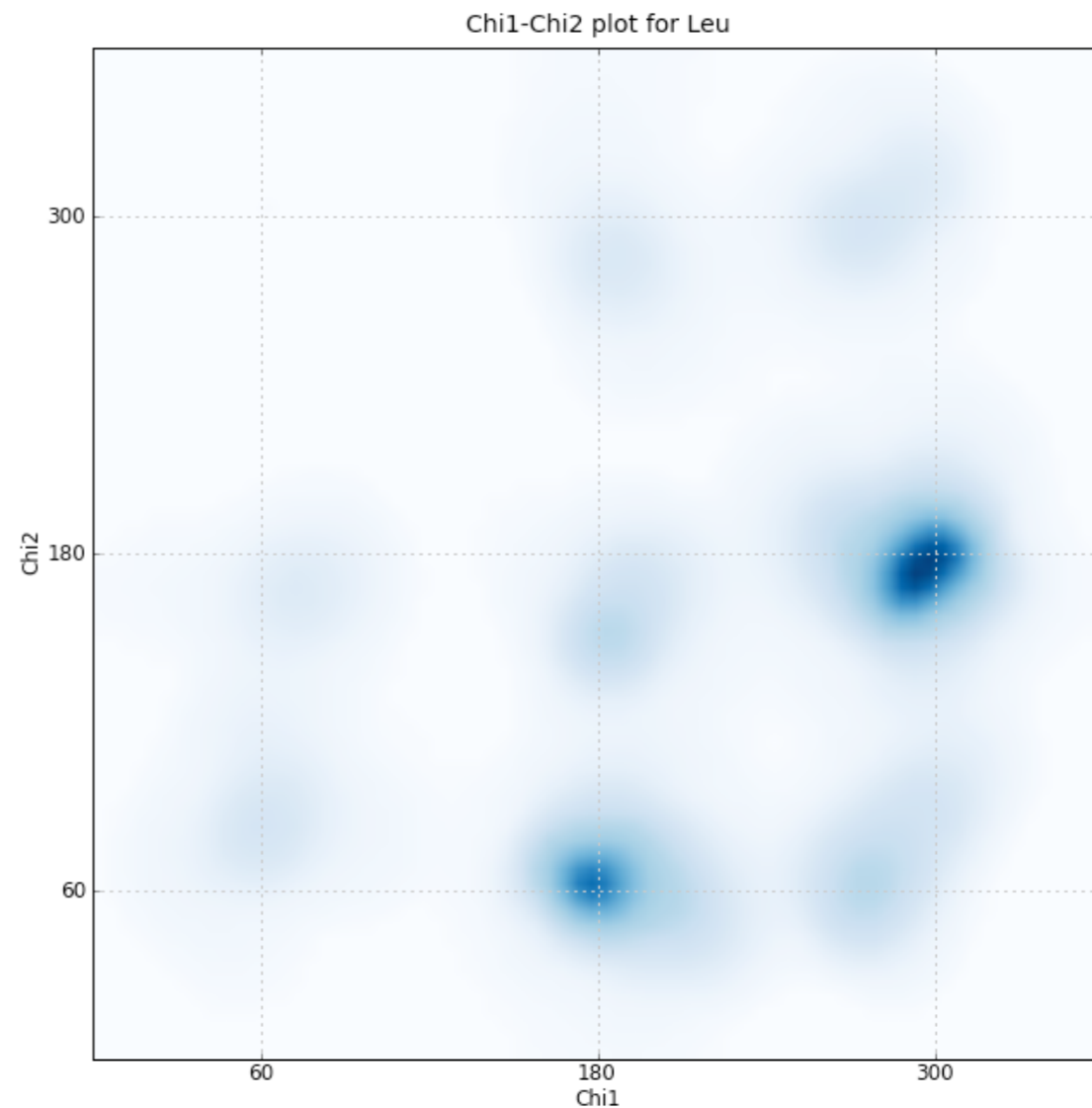


Image from Jane and David  
Richardson, Duke University

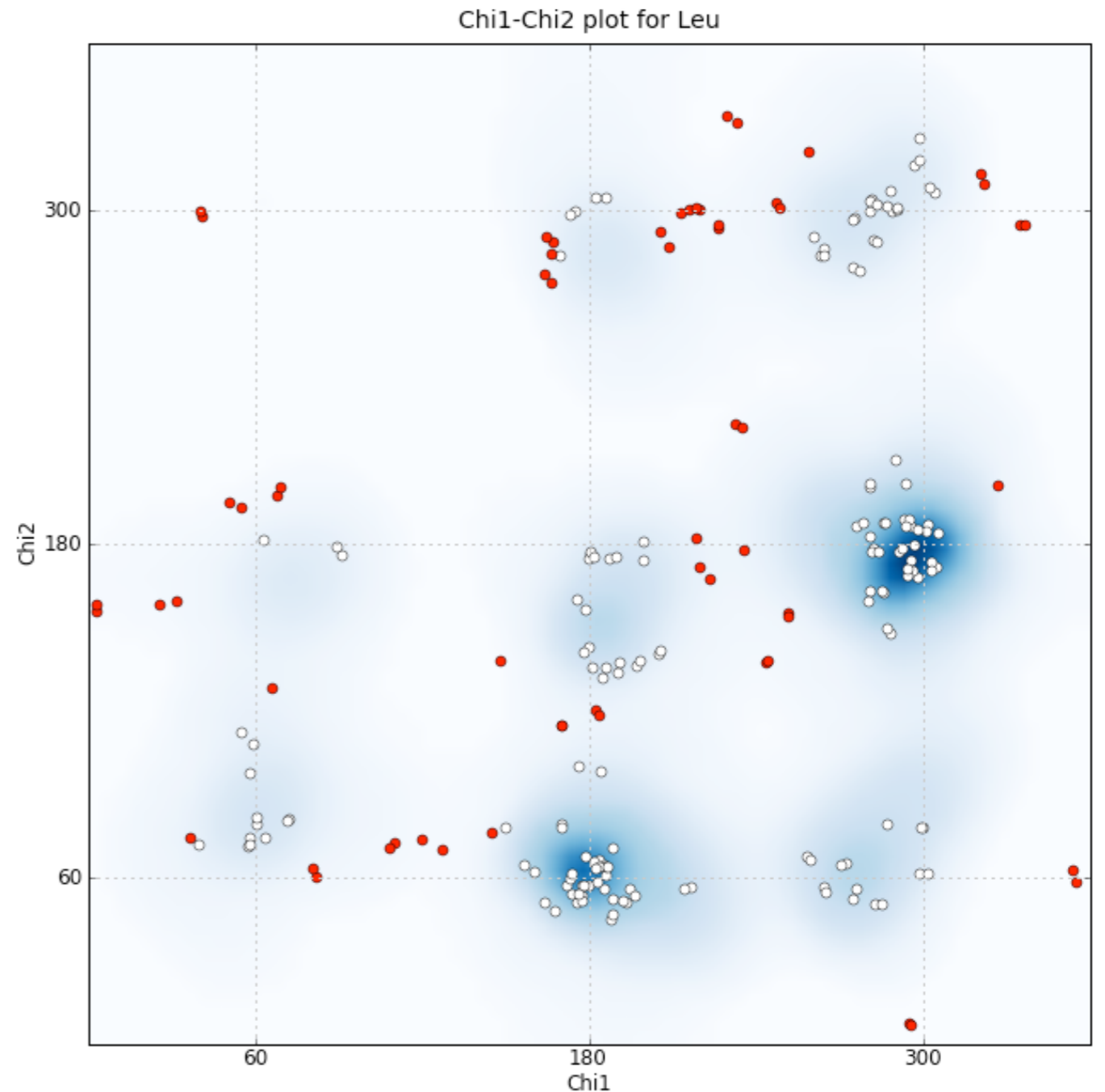


**Phenix**



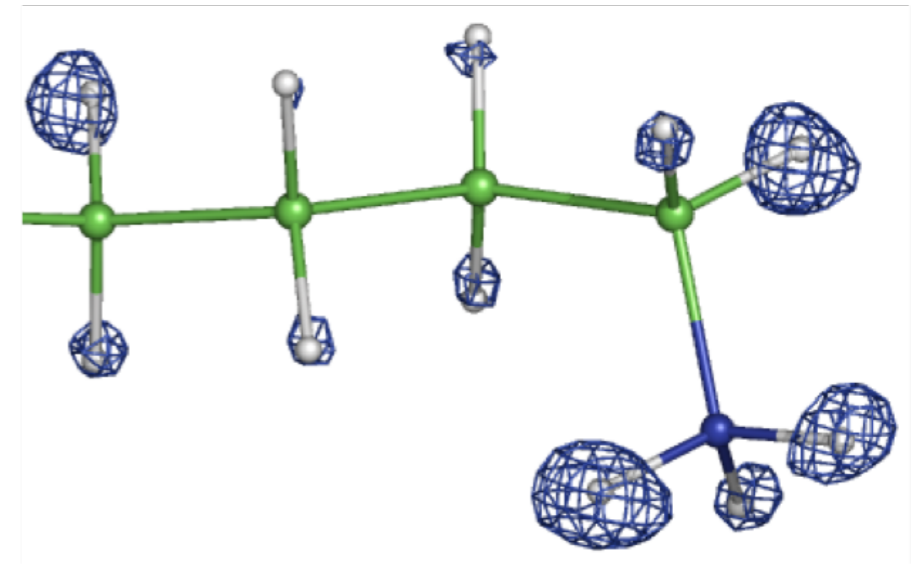
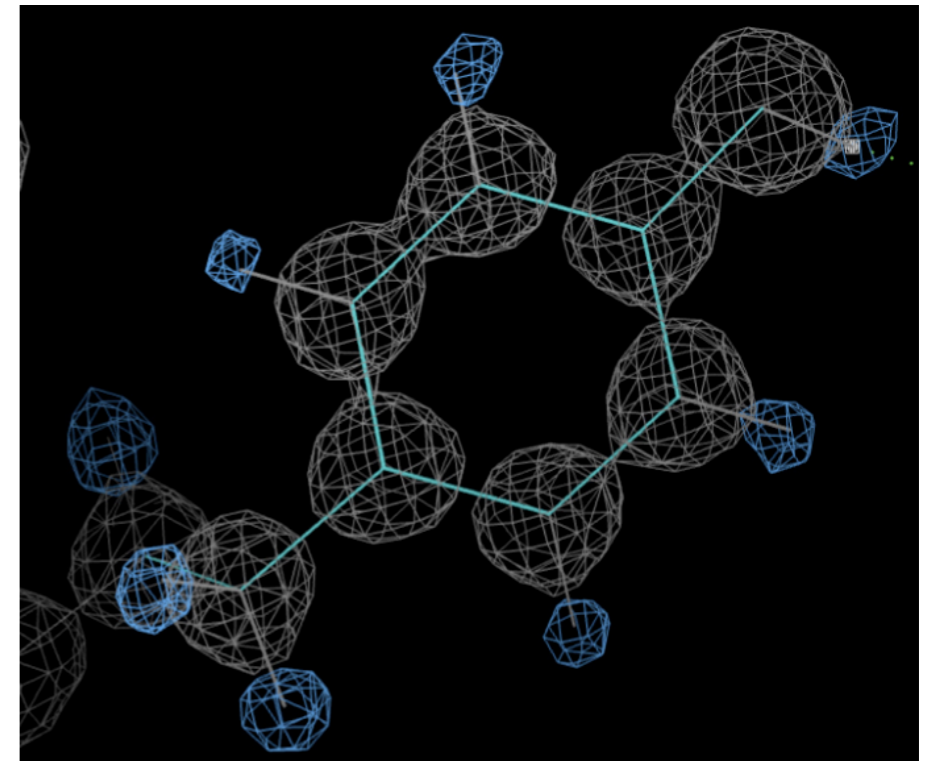
# Rotamers

- As with the Ramachandran distribution, protein side chains are expected to conform to known rotamer distributions
- More variability because of interactions with other sidechains, mainchain or ligands
- Outliers may be meaningful, but need to be verified
- Sidechains on the protein surface will often have little density (disorder)



# Hydrogens

- Macromolecules contain hydrogens
  - Approximately half of the atoms in a structure
- Hydrogens make the majority of contacts in a structure
- Typically ignored because they aren't typically seen experimentally
- But, the hydrogens are there!
- The Richardson group (Duke University) have pioneered the use of hydrogens in calculating packing (and clashes) inside macromolecules
- The quality of packing and the nature of clashes can be used to validate and correct structures



*Images from Jane and David Richardson, Duke University*

# All Atom Contacts

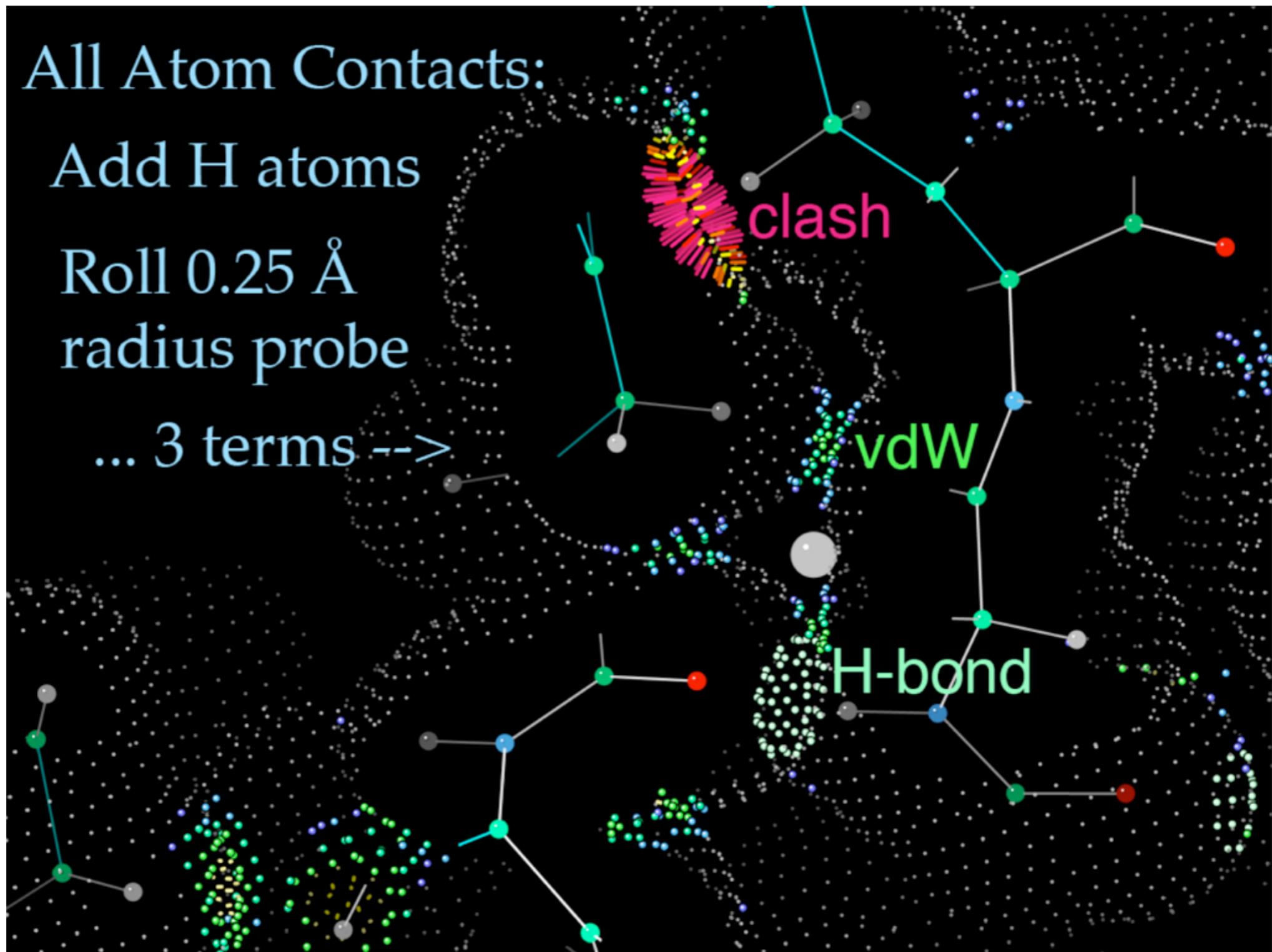


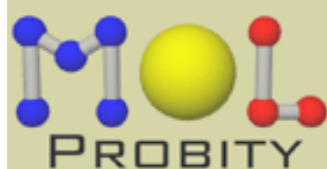
Image from Jane and David Richardson, Duke University

**Phenix**



# MolProbity

- MolProbity has been developed to validate structures (purely on coordinates)
- Performs all atom contacts, Ramachandran, rotamer and other geometry analyses



Analysis output: all-atom contacts and geometry for 3g5uH.pdb

## Summary statistics

All-Atom Contacts	Clashscore, all atoms:	159.56	2 <sup>nd</sup> percentile* (N=37, 3Å - 9999Å)
	Clashscore is the number of serious steric overlaps (> 0.4 Å) per 1000 atoms.		
Protein Geometry	Poor rotamers	20.10%	Goal: <1%
	Ramachandran outliers	11.33%	Goal: <0.2%
	Ramachandran favored	62.35%	Goal: >98%
	Cβ deviations >0.25Å	6	Goal: 0
	MolProbity score <sup>^</sup>	4.55	4 <sup>th</sup> percentile* (N=342, 3.25Å - 4.05Å)
	Residues with bad bonds:	0.04%	Goal: 0%
	Residues with bad angles:	3.85%	Goal: <0.1%

\* 100<sup>th</sup> percentile is the best among structures of comparable resolution; 0<sup>th</sup> percentile is the worst.

<sup>^</sup> MolProbity score is defined as the following:  $0.42574 \cdot \log(1 + \text{clashscore}) + 0.32996 \cdot \log(1 + \max(0, \text{pctRotOut} - 1)) + 0.24979 \cdot \log(1 + \max(0, 100 - \text{pctRamaFavored} - 2)) + 0.5$

By adding H to this model and allowing Asn/Gln/His flips, we could *automatically* improve your clashscore by 2.05 points.

<http://molprobity.biochem.duke.edu/>

  
**Phenix**



# MolProbity

- Generates detailed problem list
- Problems can be fixed more easily by using validation lists viewed visually (e.g. Coot from Phenix)

#	Res	High B	Clash > 0.4Å	Ramachandran	Rotamer	Cβ deviation	Bond lengths.	Bond angles.
		Avg: 154.80	Clashscore: 159.56	Outliers: 267 of 2356	Poor rotamers: 392 of 1950	Outliers: 6 of 2174	Outliers: 1 of 2364	Outliers: 91 of 2364
A 33	VAL	207.38	0.761Å N with A 36 LEU HD11	-	5.4% (m) chi angles: 285.2	0.04Å	-	-
A 34	SER	186.49	1.084Å HA with A 38 MET HB2	OUTLIER (0%) General case / 1.9,- 66.3	82.4% (p) chi angles: 69.5	0.015Å	-	-
A 35	VAL	204.94	1.221Å HG12 with A 359 TYR CE2	Allowed (0.14%) General case / -50.4,- 77.0	19.1% (m) chi angles: 304.1	0.049Å	-	-
A 36	LEU	142.23	1.095Å H with A 35 VAL HG23	Favored (42.64%) General case / -73.2,- 49.2	1% chi angles: 55.4,111.8	0.07Å	-	-
A 37	THR	170.59	0.723Å H with A 36 LEU HG	Favored (3.45%) General case / -69.8,- 60.5	64.9% (m) chi angles: 296.4	0.052Å	-	-
A 38	MET	155.79	1.084Å HB2 with A 34 SER HA	Favored (36.13%) General case / -49.2,- 42.4	0% chi angles: 229.3,294.4,131.7	0.054Å	-	-
A 39	PHE	122.57	1.127Å HB2 with A 35 VAL O	Favored (49.78%) General case / -51.0,- 39.2	31.2% (t80) chi angles: 196.6,84	0.027Å	-	-
A 40	ARG	102.85	0.683Å N with A 37 THR O	Allowed (0.94%) General case / - 116.3,69.9	9.1% (mtp180) chi angles: 248.9,176.6,56.5,191.6	0.078Å	-	-
			0.484Å	Allowed (0.6%)	0.5%			

# Results - Rebuilding and Validation

The screenshot displays the Coot 0.8.9.1 EL interface. On the left, a 3D molecular model is shown with atoms as spheres and bonds as sticks, overlaid on a blue mesh representing the electron density map. The model is colored by element: carbon in cyan, oxygen in red, and nitrogen in blue. The right panel shows the 'Validation' results for 'RealSpaceRefine\_1'.

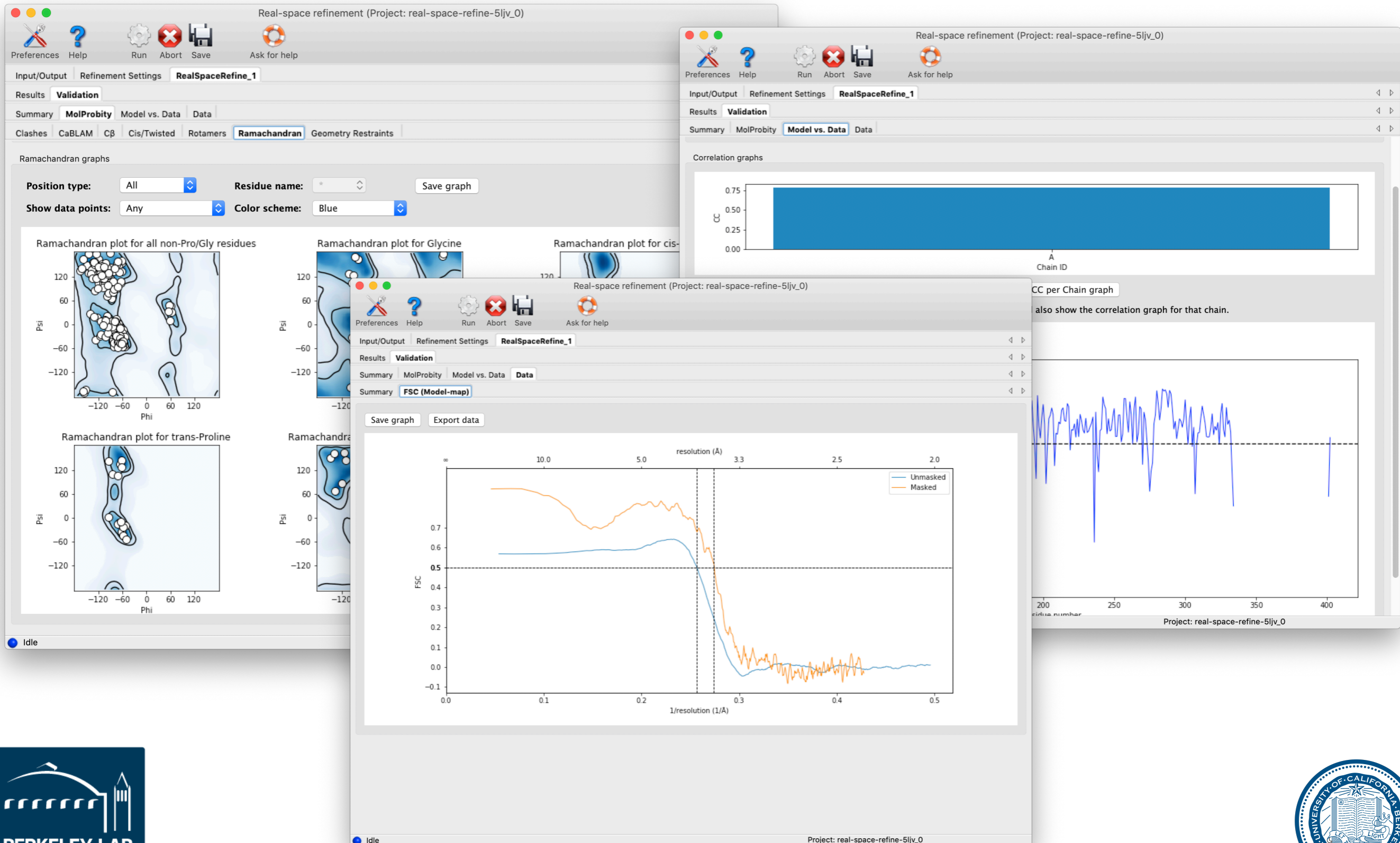
**Validation Results Summary:**

Model		Data		
Composition (#)		Box		
Chains	2	Lengths (Å)	49.58, 68.34, 80.40	
Atoms	2500 (Hydrogens: 0)	Angles (°)	90.00, 90.00, 90.00	
Residues	Protein: 325 Nucleotide: 0	Supplied Resolution (Å)	3.7	
Water	0	Resolution Estimates (Å)	Masked	Unmasked
Ligands	MG: 1 ADP: 1	d FSC (half maps; 0.143)	---	---
Bonds (RMSD)		d 99 (full/half1/half2)	3.7/---/---	3.2/---/---
Length (Å) (# > 4σ)	0.005 (0)	d model	3.7	3.7
Angles (°) (# > 4σ)	0.754 (0)	d FSC model (0/0.143/0.5)	3.2/3.4/3.6	3.4/3.6/3.9
MolProbity score	1.81	Man min/max/mean	-0.42/0.80/0.03	
Clash score	10.33	<b>Model vs. Data</b>		
Ramachandran plot (%)		CC (mask)	0.81	
Outliers	0.00	CC (box)	0.57	
Allowed	4.02	CC (peaks)	0.40	
Favored	95.98	CC (volume)	0.78	
Rotamer outliers (%)	0.00	Mean CC for ligands	0.73	
Cβ outliers (%)	0.00			
Peptide plane (%)				
Cis proline/general	5.6/0.0			
Twisted proline/general	0.0/0.0			
CaBLAM outliers (%)	2.18			
ADP (B-factors)				
Iso/Aniso (#)	2500/0			
min/max/mean				
Protein	38.70/81.46/52.85			
Nucleotide	---			
Ligand	48.04/49.31/48.09			
Water	---			
Occupancy				
Mean	1.00			

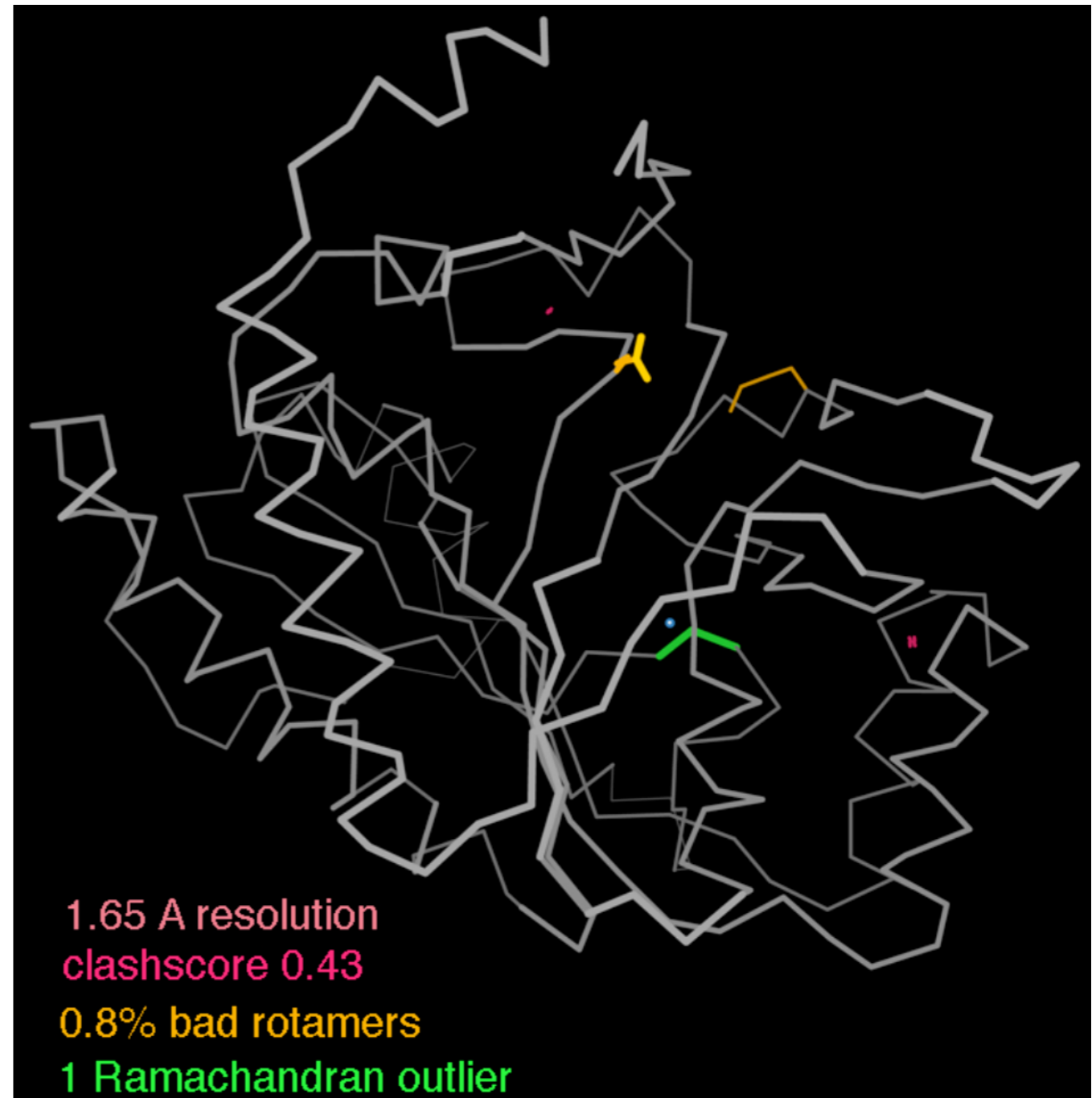
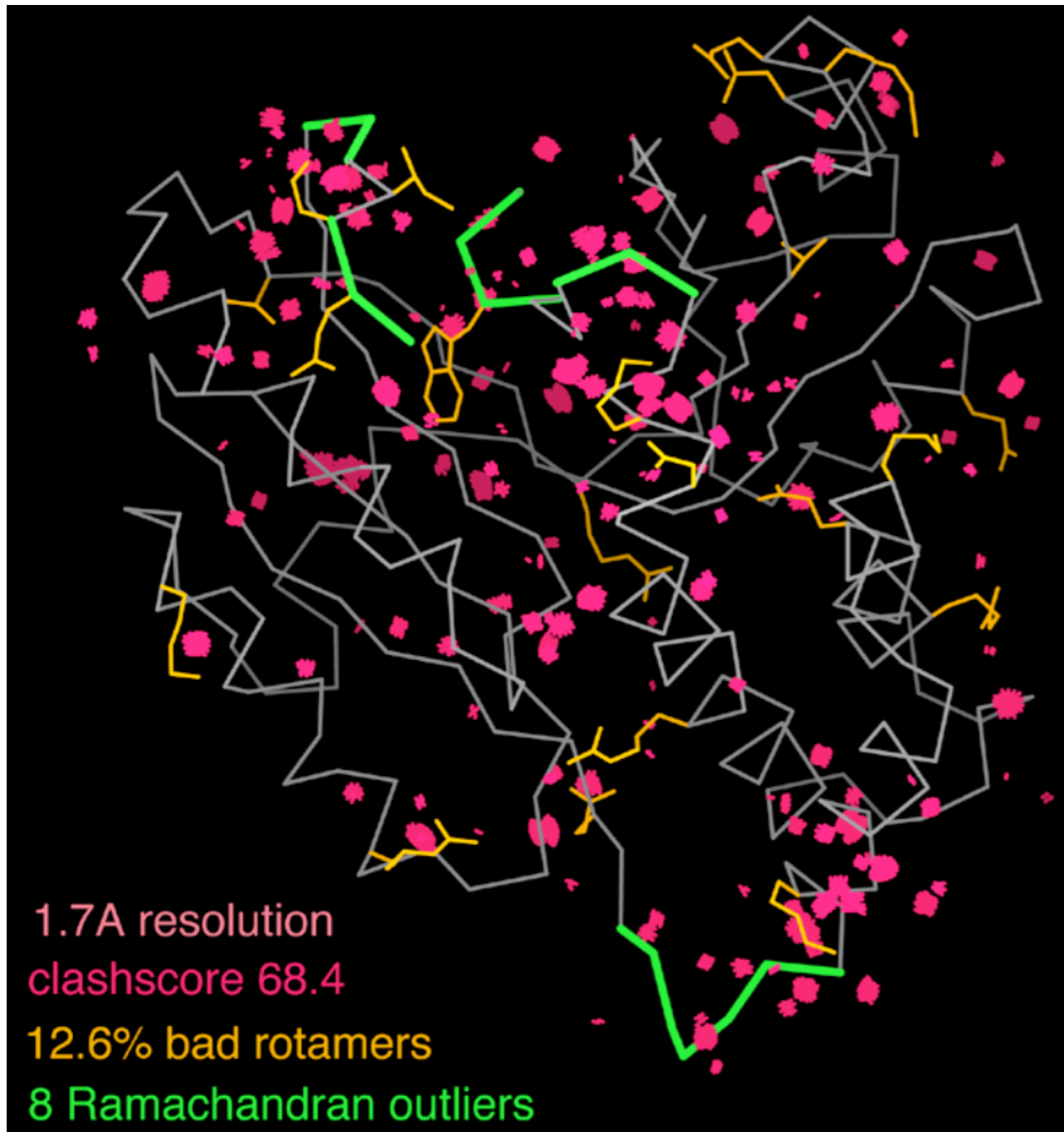


# Validation

- Outlier lists recenter Coot view; Probe dots automatically loaded



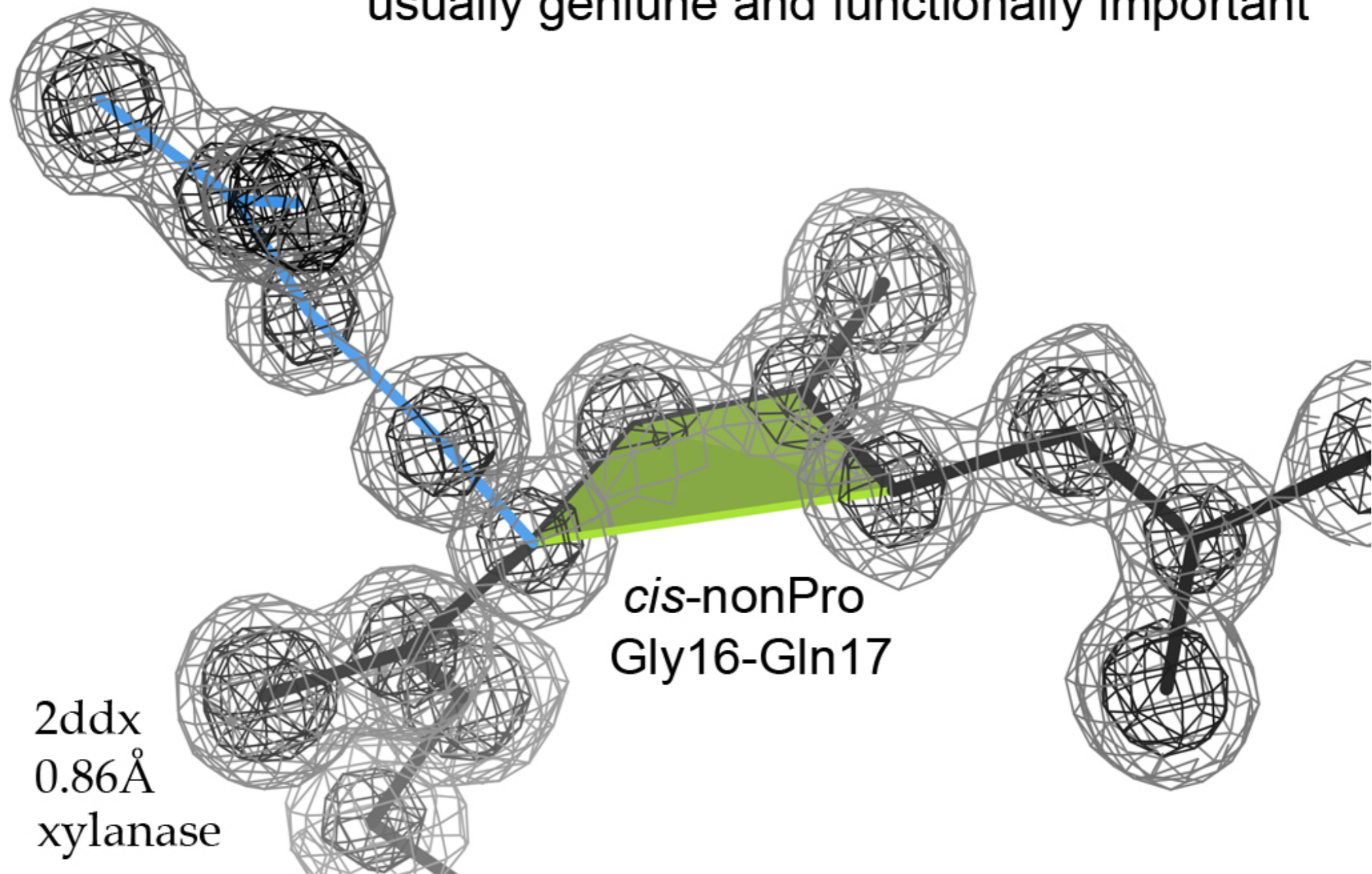
# Using Validation Tools Improves Models



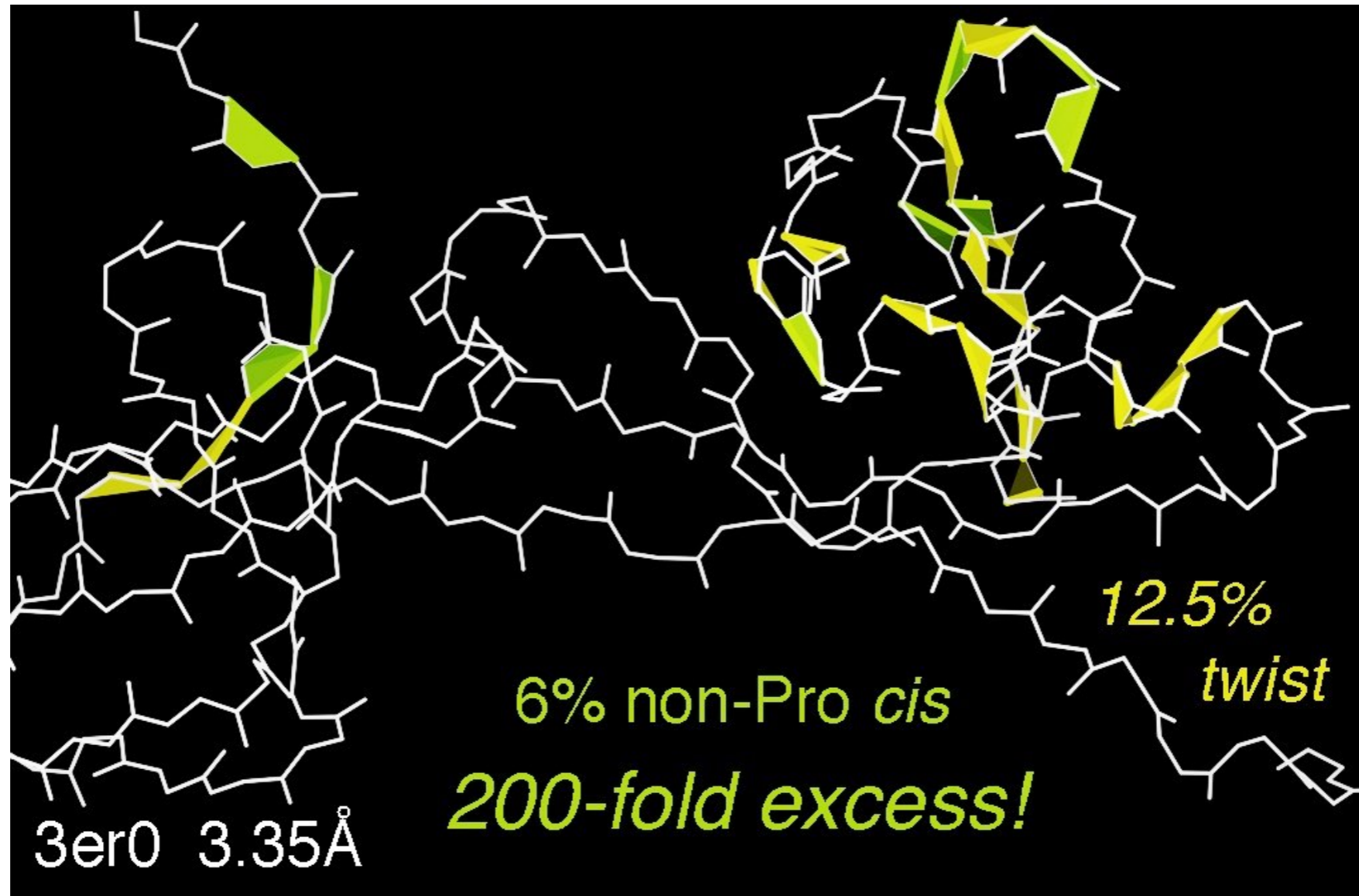
Images from Jane and David Richardson, Duke University

# Cis-Peptides

*cis*-nonPro peptides are very rare (~0.03%),  
usually genuine and functionally important



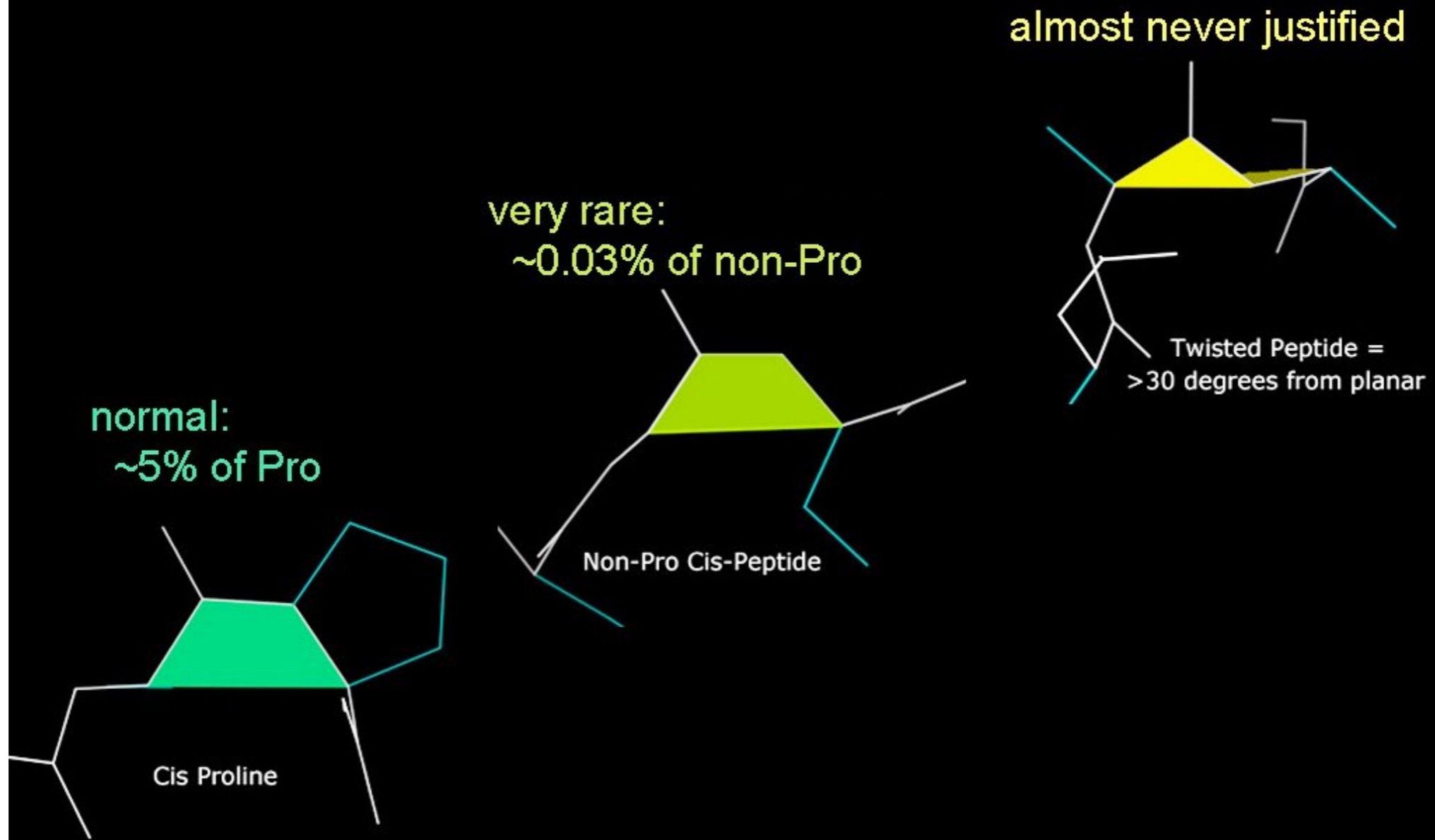
# Too Many Cis-Peptides



- Cis non-Prolines are chosen much more often than chance, because they are more compact than trans and fit better into the shrunken & rather featureless low-resolution density (esp. for loops).
- Automated building with a no-cis fragment library (Tom Terwilliger)

# Omegalyze

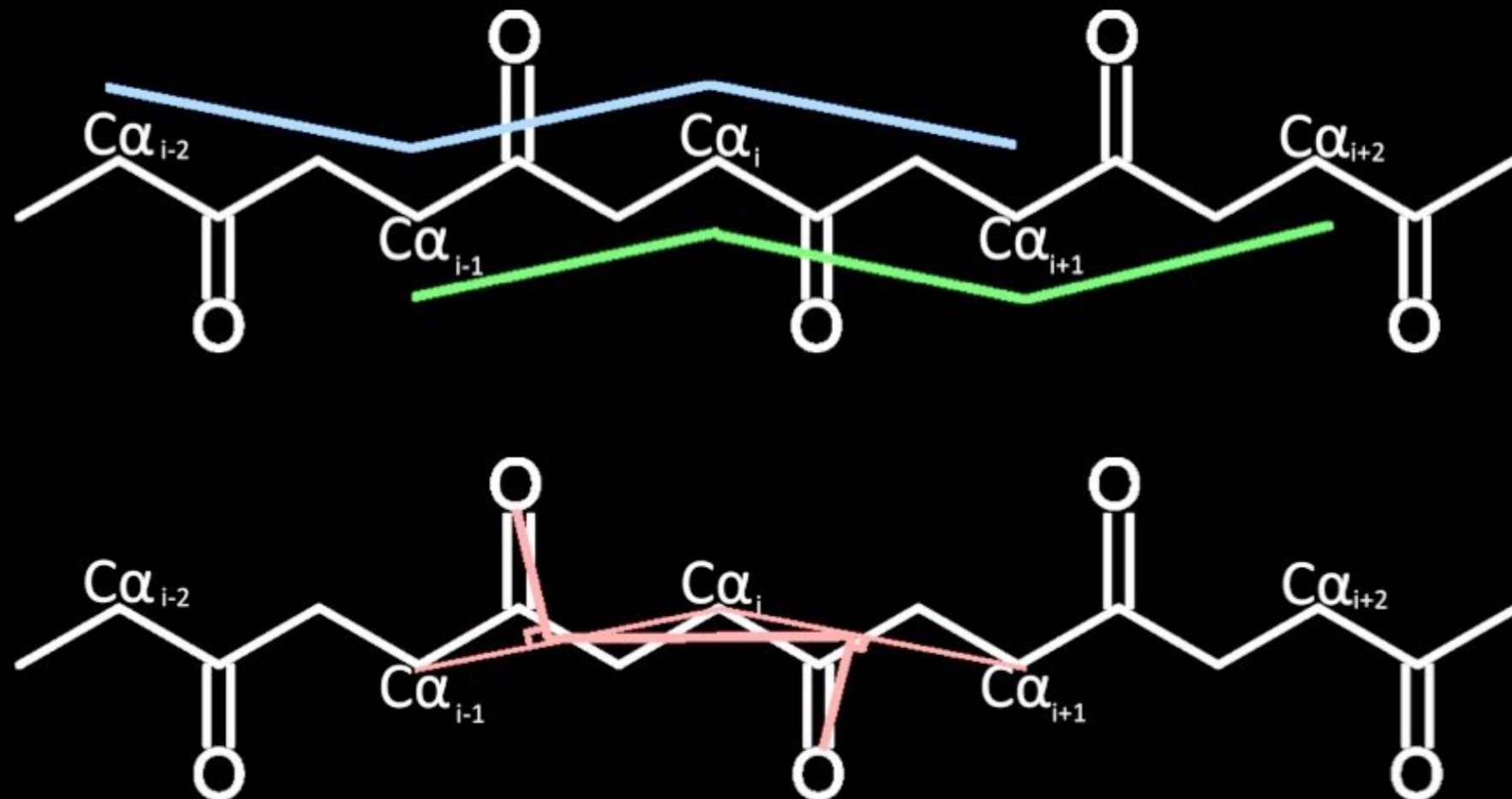
Flagging non-Pro *cis* & twisted peptides in Omegalyze



# Validation Using $C\alpha$ Atoms

## CaBLAM Parameter Space

A minimalist alternative



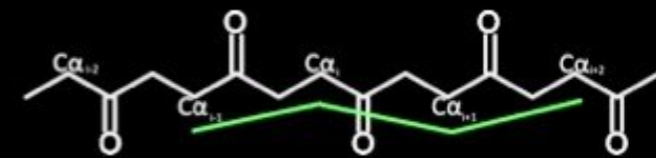
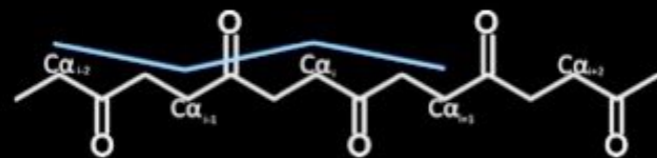
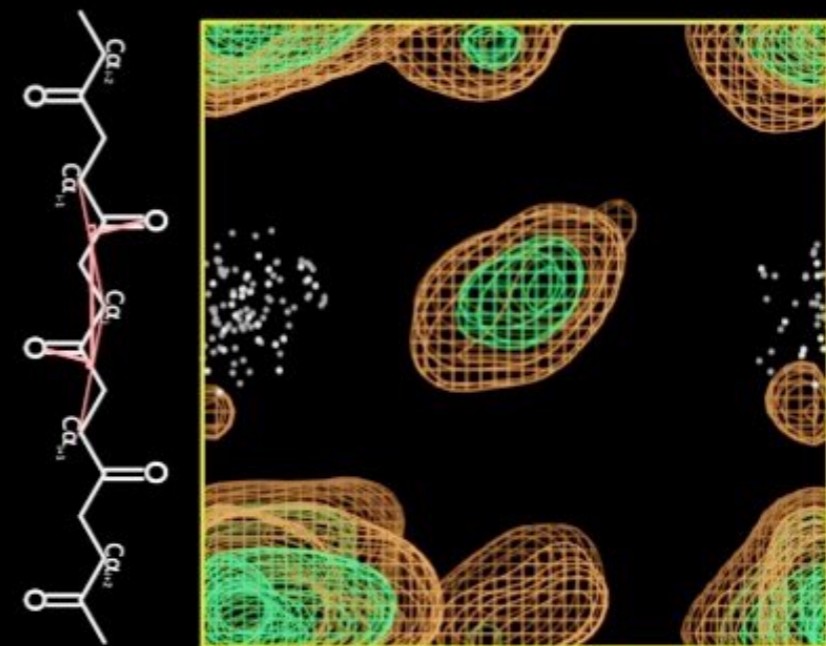
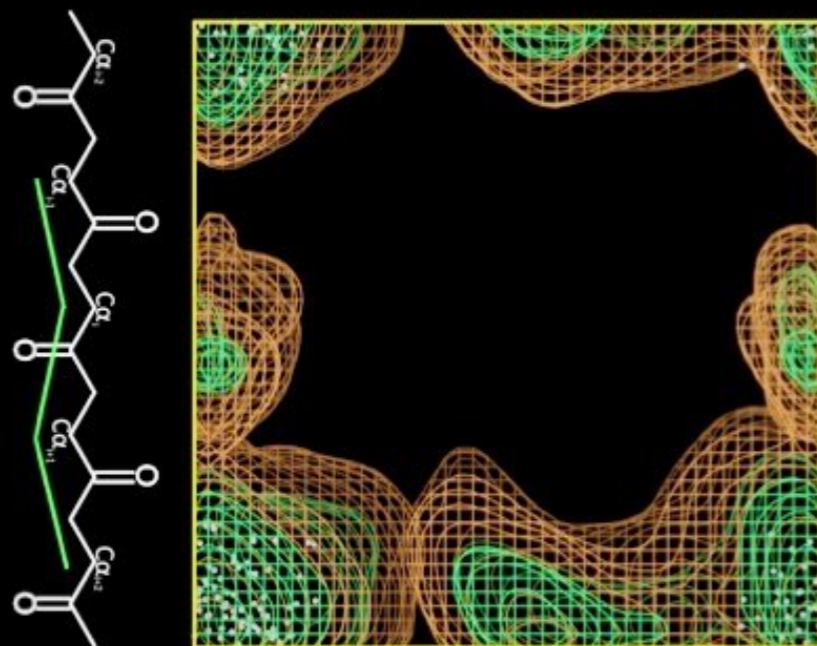
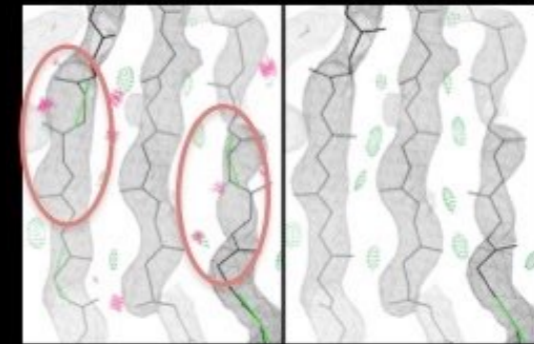
**Phenix**

Christopher Williams,  
Duke University

# Identifying Distorted Secondary Structure

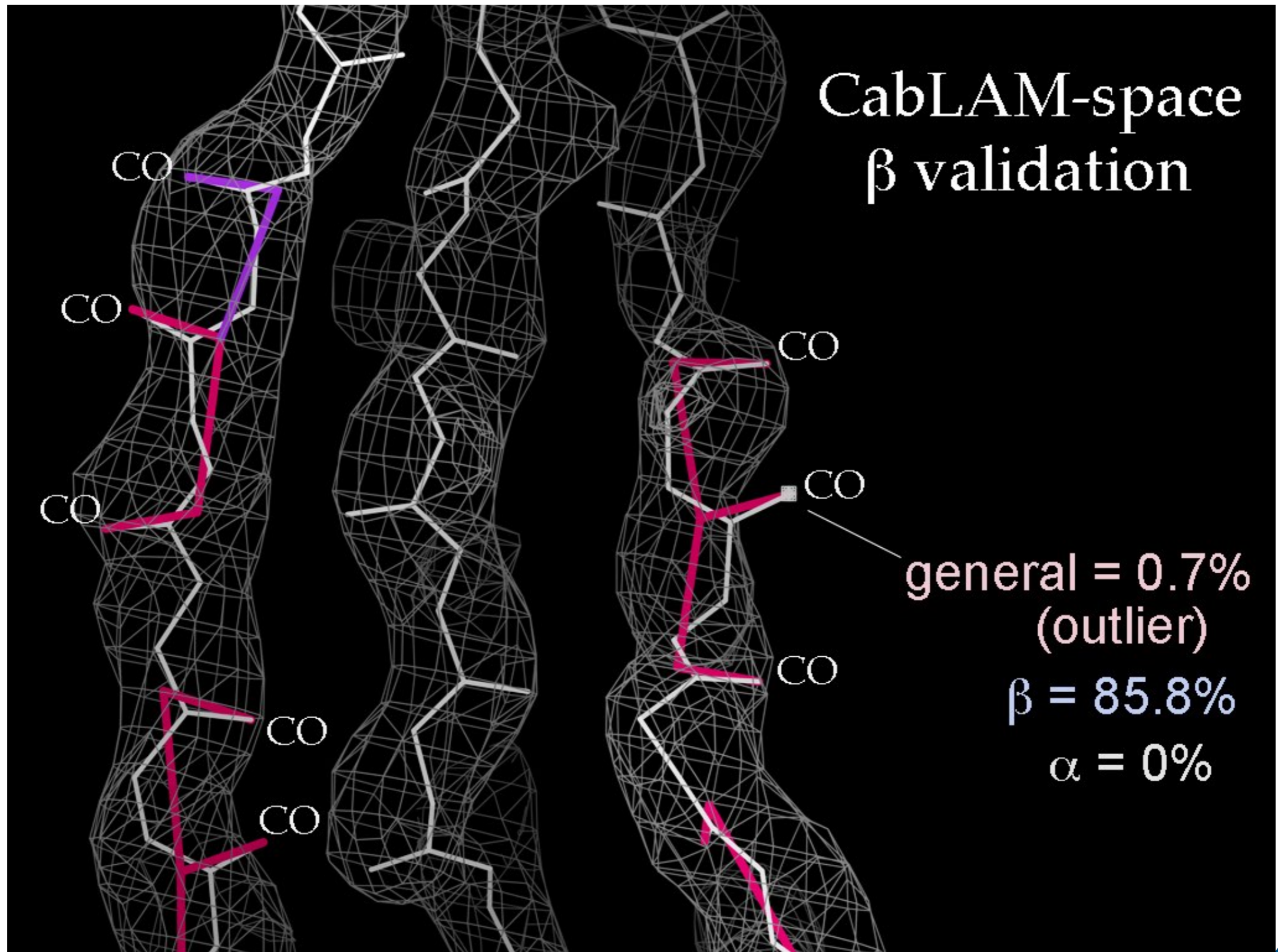
## Diagnosing Strands

Pathological strands from 70S Ribosome



Christopher Williams,  
Duke University

# Assessing Secondary Structure Probability





# Comprehensive Validation

The screenshot displays the Phenix Comprehensive Validation interface for a CryoEM project. The main window is titled "Comprehensive validation (CryoEM) (Project: rea-space-refine-6crz)". The interface is divided into several sections:

- Summary:** Shows the model and map paths, and an "Open in Coot" button.
- Model:** Contains a table of MolProbity and CaBLAM statistics.
- MolProbity:** Provides a detailed overview of MolProbity scores and a table of outliers.
- CaBLAM:** Shows CaBLAM outlier statistics and a table of outliers.
- C $\beta$  deviation analysis:** Reports on C $\beta$  position outliers.
- Cis and twisted peptides:** Reports on cis conformations and non-trans peptides.

**MolProbity Summary:**

MolProbity score	1.72
Clash score	5.44
Rotamer outliers (%)	0.00 (Goal: < 1%)
C $\beta$ outliers	0 (Goal: 0)

**CaBLAM Summary:**

Outliers (%)	3.88	Disfavored (%)	8.96	C $\alpha$ outliers (%)	1.19
--------------	------	----------------	------	-------------------------	------

**MolProbity Outliers Table:**

Chain	Residue	Evaluation	CaBLAM Score	CA Geometry Score	Secondary Structure
A	ILE 955	CaBLAM Disfav...	0.03762	0.01447	
A	PRO 969	CaBLAM Disfav...	0.02931	0.46424	try alpha helix
A	SER 1012	CaBLAM Outlier	0.00273	0.67504	try alpha helix
A	LEU 1016	CaBLAM Outlier	0.00086	0.07553	

**CaBLAM Outliers Table:**

Chain	Residue	Evaluation	CaBLAM Score	CA Geometry Score
A	ILE 955	CaBLAM Disfav...	0.03762	0.01447
A	PRO 969	CaBLAM Disfav...	0.02931	0.46424
A	SER 1012	CaBLAM Outlier	0.00273	0.67504
A	LEU 1016	CaBLAM Outlier	0.00086	0.07553

**C $\beta$  deviation analysis:** No C $\beta$  position outliers detected.

**Cis and twisted peptides:** No non-trans peptides detected.

# Map Resolution and Map/Model Fit

Summary of map resolution estimates.

Metric	Objects used	Purpose	Values	Meaning, possible actions
$d_{\text{FSC}}$	Half-maps	Highest resolution at which the experimental data are confident	The higher the better	Resolution determined using half-maps method
$d_{99}$	Map	Resolution cutoff beyond which Fourier coefficients are negligibly small	$d_{99} \geq d_{\text{FSC}}$ $d_{99} < d_{\text{FSC}}$ $d_{99} \gg d_{\text{FSC}}$	Expected values Verify $d_{\text{FSC}}$ ; omit coefficients with $d_{99} \leq d < d_{\text{FSC}}$ Sharpen the map
$d_{\text{model}}$	Map and model	Resolution cutoff at which the model map is the most similar to the target map	$d_{\text{model}} \geq d_{\text{FSC}}$ $d_{\text{model}} < d_{\text{FSC}}$ $d_{\text{model}} \gg d_{\text{FSC}}$ $d_{\text{model}} \ll d_{99}$ $d_{\text{model}} \gg d_{99}$	Expected values Verify $d_{\text{FSC}}$ ; check ADP (too large?); validate map details Sharpen the map Check ADP (too large?) Check ADP (too small?); check the model
$d_{\text{FSC\_model}}$	Map and model	Resolution cutoff up to which the model and map Fourier coefficients are similar	$d_{\text{FSC\_model}} \geq d_{\text{FSC}}$ $d_{\text{FSC\_model}} < d_{\text{FSC}}$ $d_{\text{FSC\_model}} \geq d_{\text{FSC}}$ $d_{\text{FSC\_model}} \gg d_{\text{model}}$ $d_{\text{FSC\_model}} \ll d_{\text{model}}$	Expected values Verify $d_{\text{FSC}}$ ; omit coefficients with $d_{\text{FSC\_model}} \leq d < d_{\text{FSC}}$ Sharpen the map Omit coefficients with $d_{\text{model}} \leq d < d_{\text{FSC\_model}}$ Sharpen the map

Summary of map correlation coefficients used in this work.

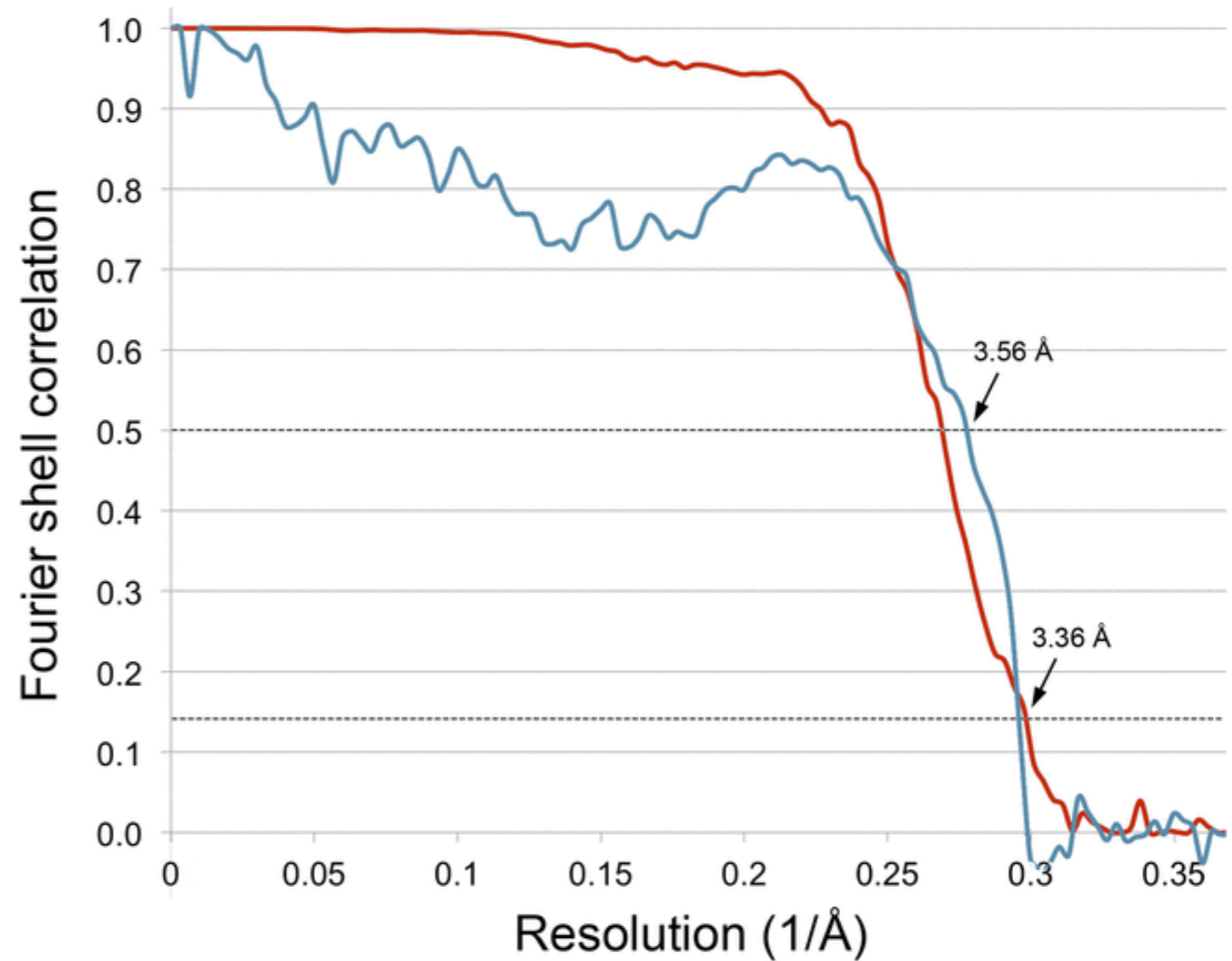
Metric	Region of the map used in calculation	Purpose
$\text{CC}_{\text{box}}$	Whole map	Similarity of maps
$\text{CC}_{\text{mask}}$	Jiang & Brünger (1994) mask with a fixed radius	Fit of the atomic centers
$\text{CC}_{\text{volume}}$	Mask of points with the highest values in the model map	Fit of the molecular envelope defined by the model map
$\text{CC}_{\text{peaks}}$	Mask of points with the highest values in the model and in the target maps	Fit of the strongest peaks in the model and target maps
$\text{CC}_{\text{vr\_mask}}$	Same as $\text{CC}_{\text{mask}}$ but atomic radii are variable and function of resolution, atom type and ADP	Fit of the atomic images in the given map

Afonine et al: New tools for the analysis and validation of cryo-EM maps and atomic models. *Acta Cryst.* 2018, **D74**:814-840.



# Resolution Determination

$$FSC(r) = \frac{\sum_{r_i \in r} F_1(r_i) \cdot F_2(r_i)^*}{\sqrt{\sum_{r_i \in r} |F_1(r_i)|^2 \cdot \sum_{r_i \in r} |F_2(r_i)|^2}}$$



# Cross Validation with Half Maps

- Perturb model (random shift of coordinates)
- Re-refine against 1 half map
- Calculate FSC of model against 2nd half map
- FSC curve shouldn't show signal beyond the half map resolution

# Model/Map Validation

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**Ray Yu-Ruei Wang, Frank DiMaio**

University of Washington

**Nat Echols**

Lawrence Berkeley National Laboratory

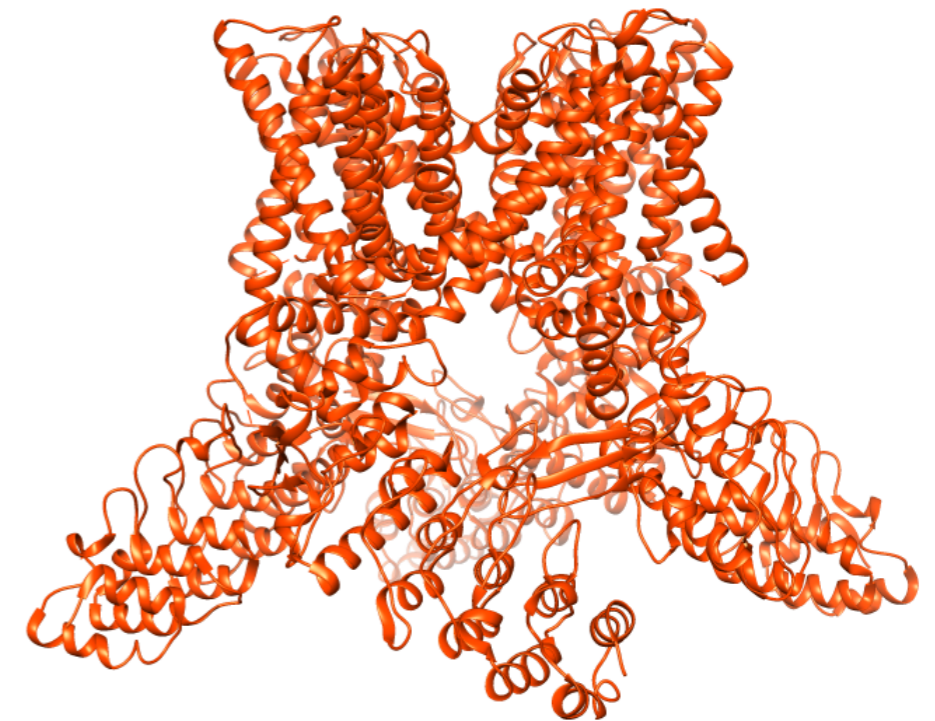
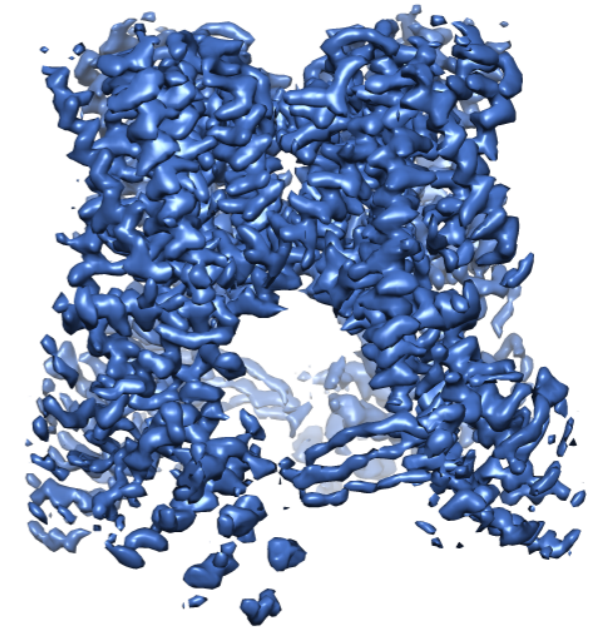


University of California  
San Francisco



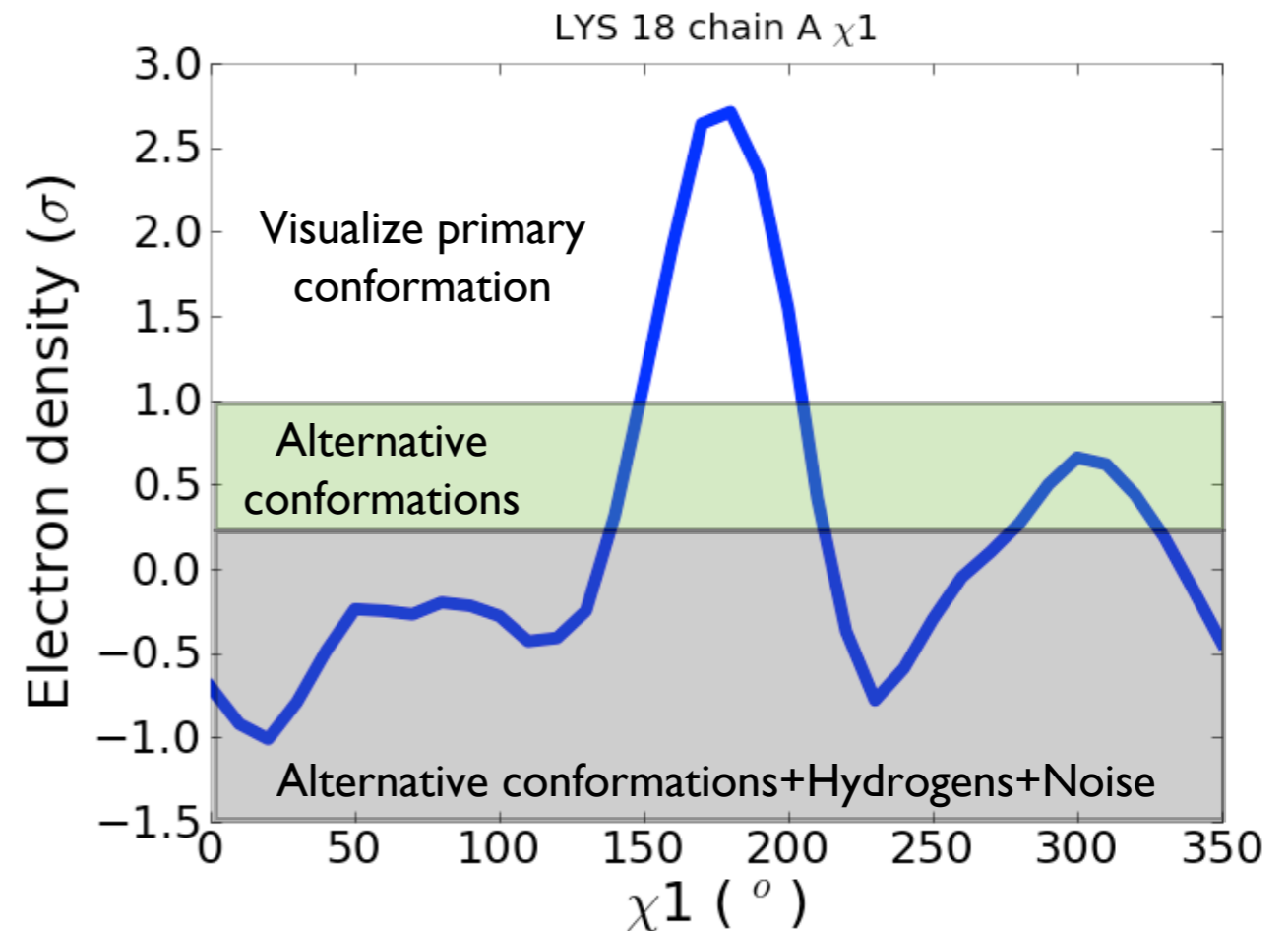
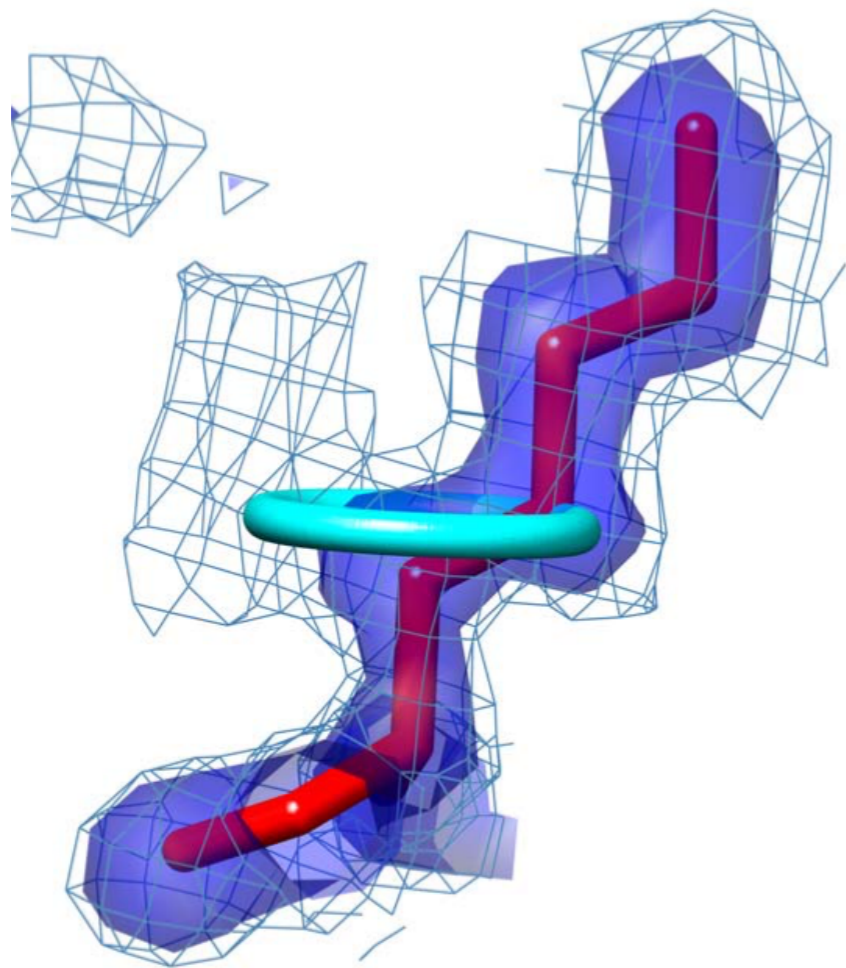
# Validation and Cryo-EM

- Do the map make sense?
- Gold Standard FSC of half maps
- Does the model make sense?
  - MolProbity
- Does the model fit the map?
  - Overall and local density correlation
  - What about the detailed local fit?



# Look at the Density Around Sidechains

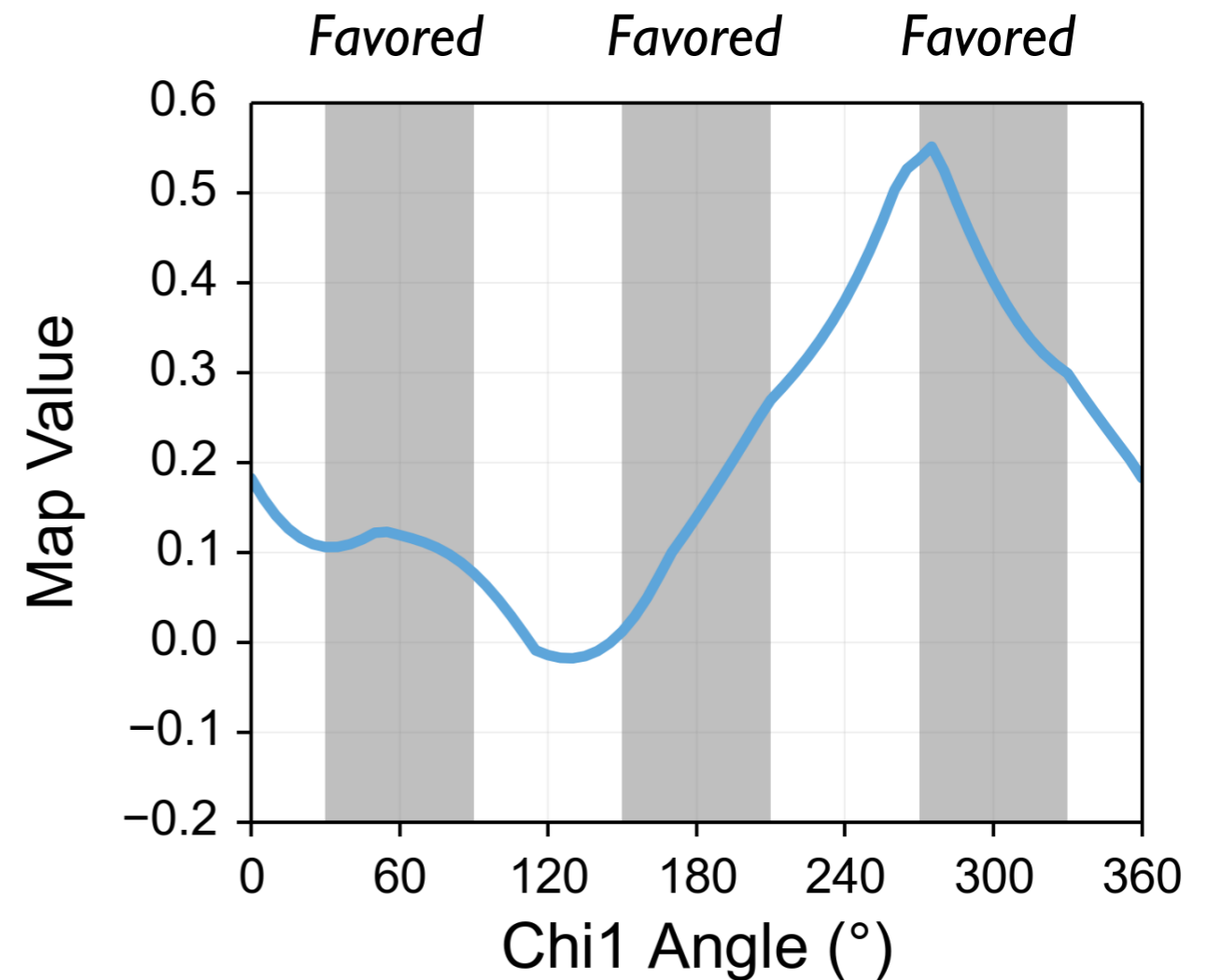
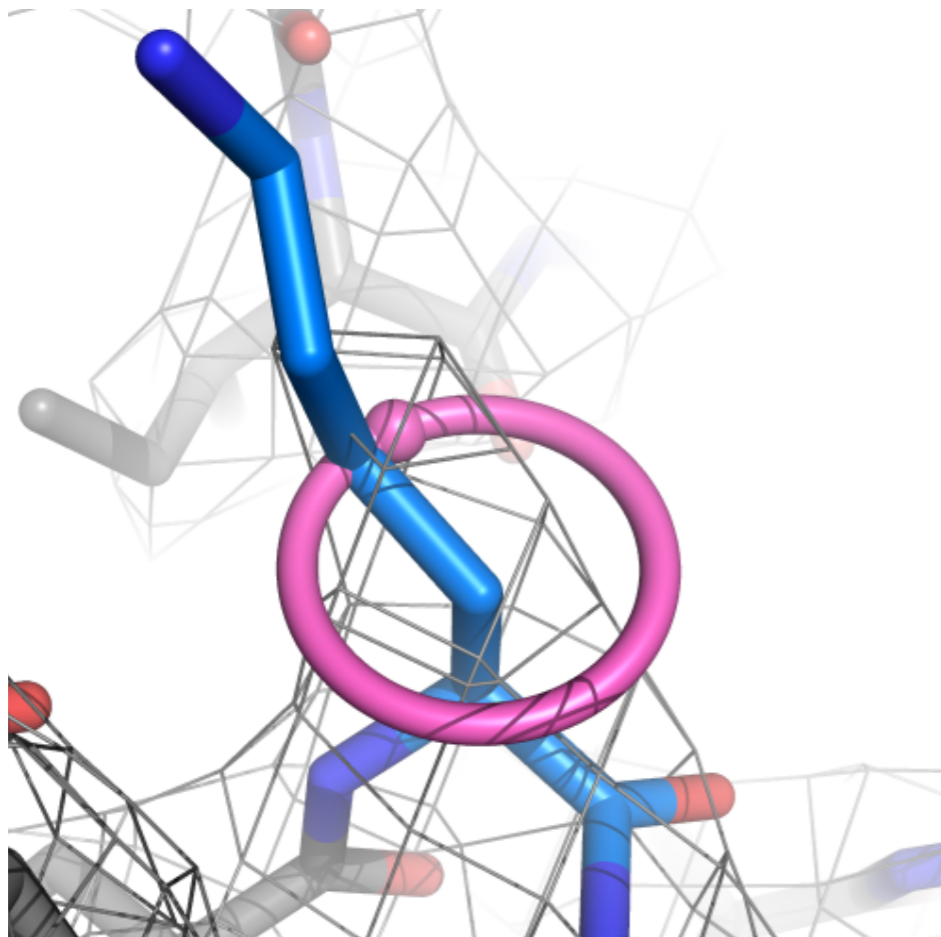
## Ringer



Lang PT, et al. Automated electron-density sampling reveals widespread conformational polymorphism in proteins. *Protein Science*. 2010.

# Look at the Density Around Sidechains

*EMRinger*



Barad BA, et al. EMRinger: Side-chain-directed model and map validation for 3D Electron Cryomicroscopy. *Nature Methods*. 2015

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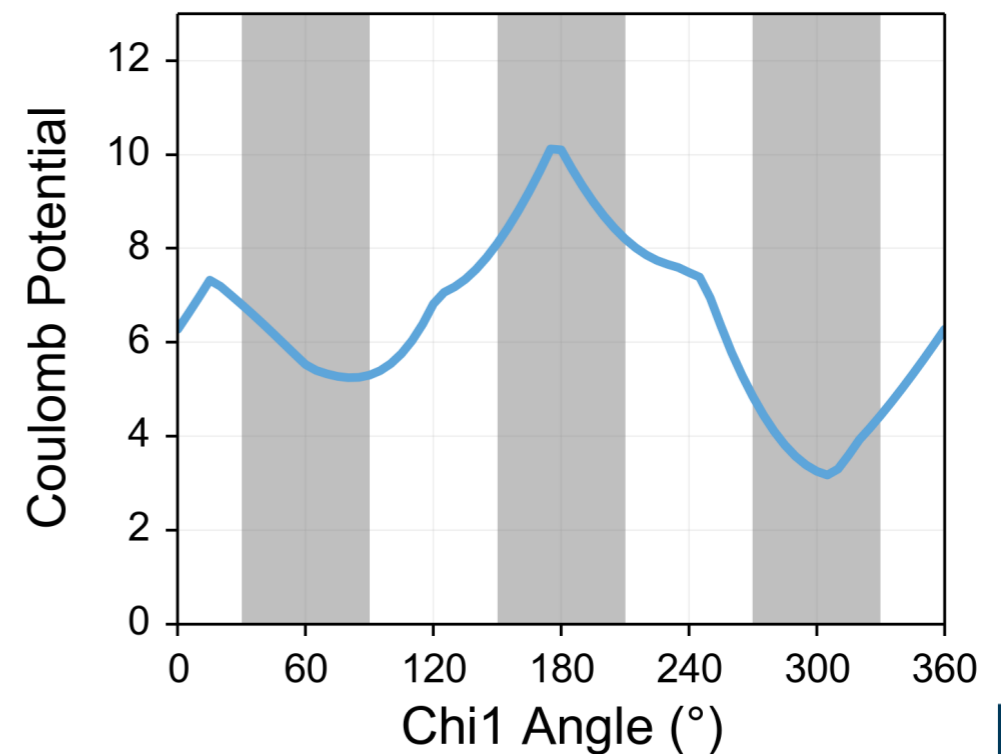
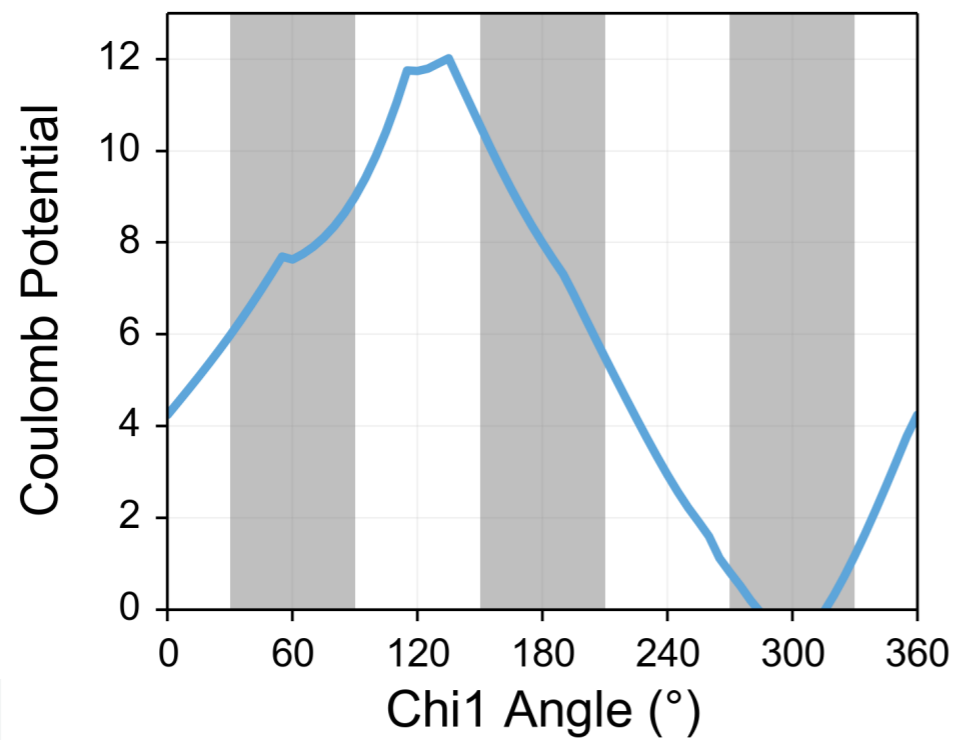
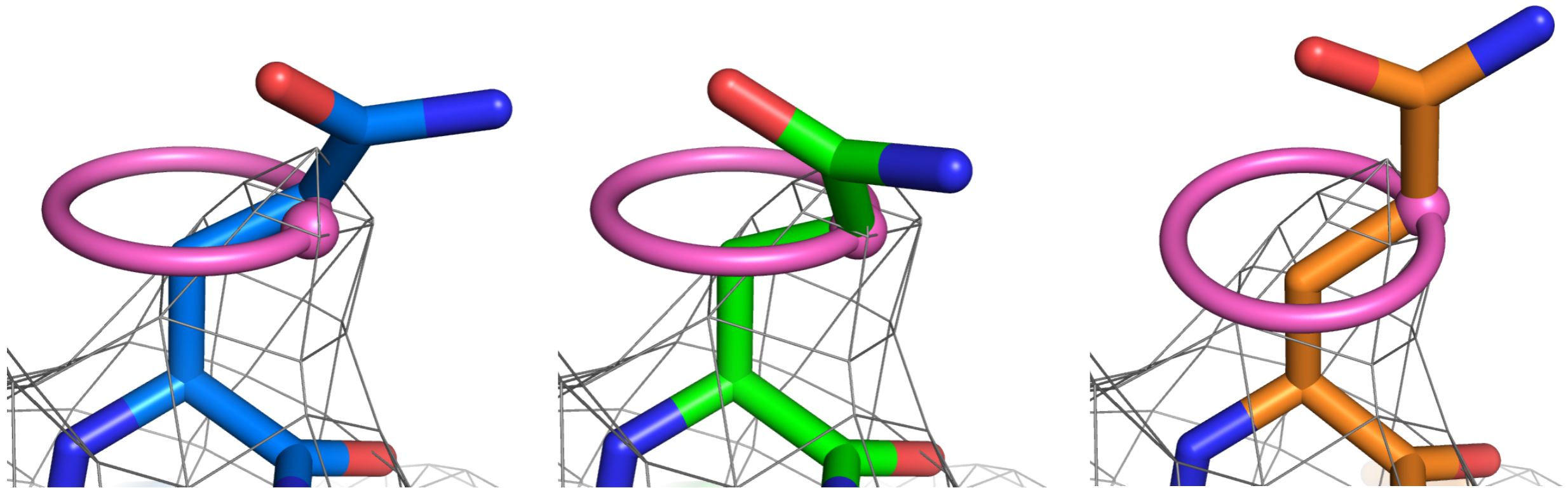
Phenix

Ben Barad, Jaime Fraser, UCSF



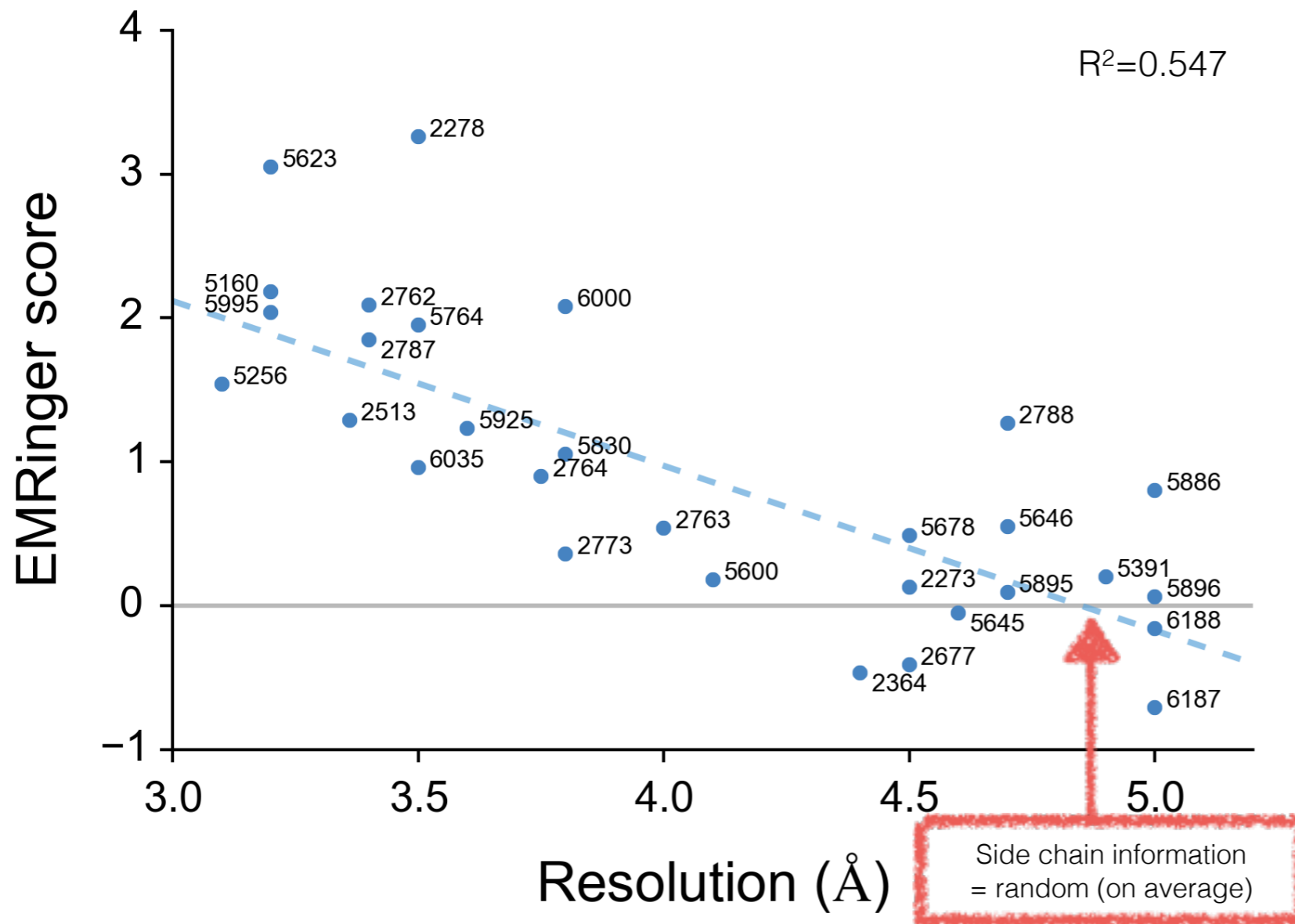


# EMRinger reports on backbone placement



# EMRinger Score to Validate Model vs Data

- Quantify how well the model backbone puts side chains in places where there are density peaks consistent with rotameric conformations



<http://emringer.com>

**Phenix**

- Available in GUI and command line
- `phenix.emringer`  
`model.pdb`  
`map.ccp4`

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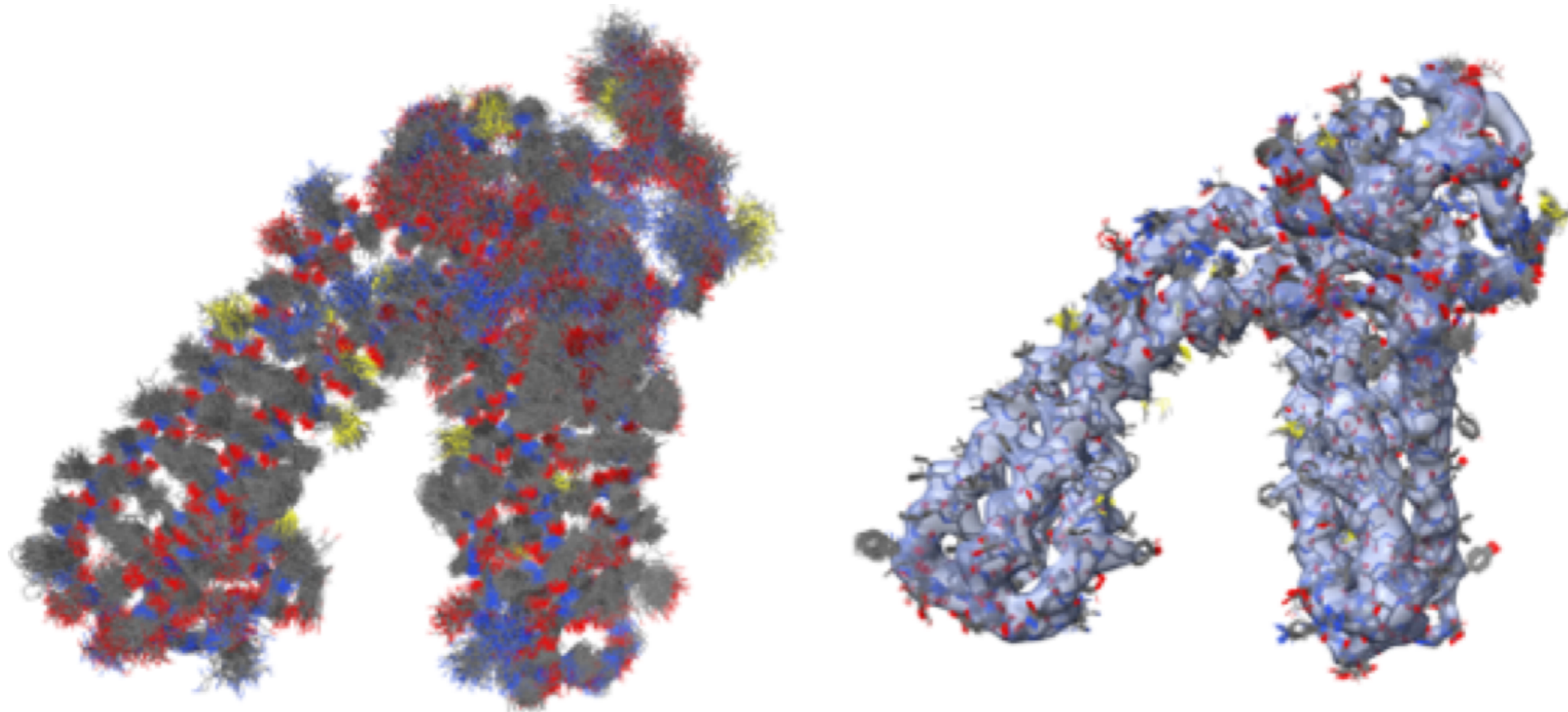
**Phenix**

Ben Barad, Jaime Fraser, UCSF



# Ensembles

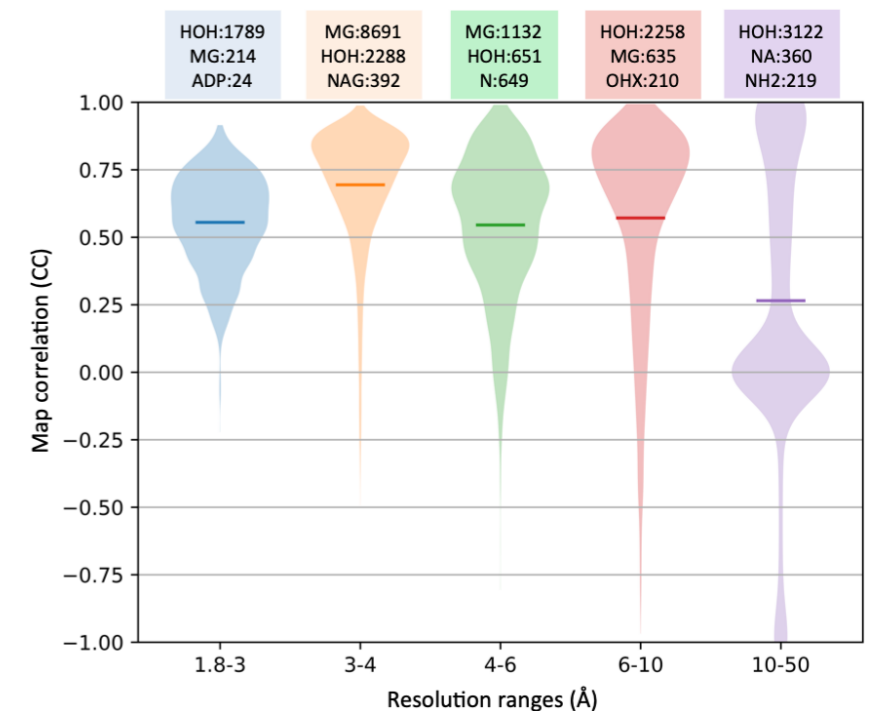
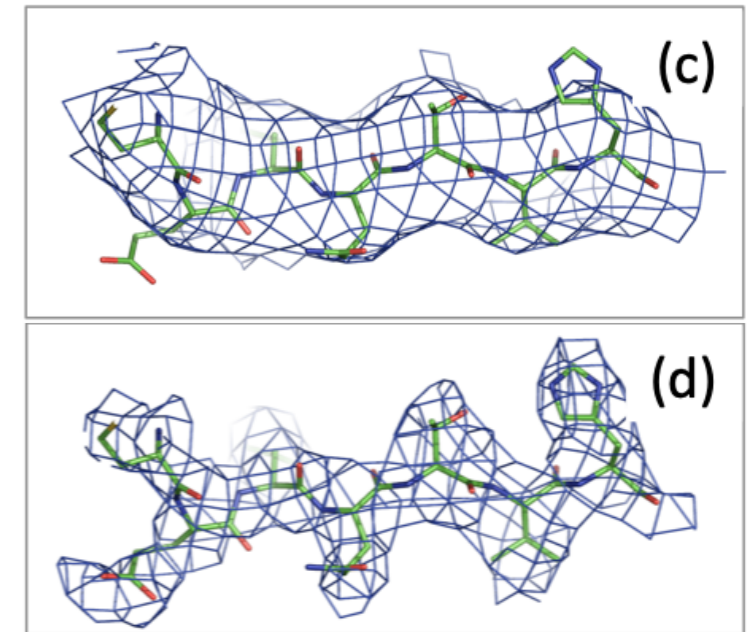
- At lower resolution ensemble models are probably more appropriate
- Can be used to help assess map variability (Herzik, Fraser, Lander. Structure. 2019)



# Deposition Issues

- Successful re-analysis of cryo-EM data relies on accurate data/model deposition
- Current practice has led to significant issues:
  - Models misplaced wrt maps
  - Inconsistent map deposition (sharpened, masked, filtered, wrong map)
  - Absence of half-maps
  - Very variable assessments of resolution
  - Optimistic ligand placement (probably unintentional)

Afonine et al: New tools for the analysis and validation of cryo-EM maps and atomic models.  
*Acta Cryst.* 2018, **D74**:814-840.



# Conclusions

- Many of the validation metrics developed to assess models can be readily applied to cryo-EM structures
- Many of the pitfalls of low resolution from other fields apply to cryo-EM
- Care needs to be taken to ensure that validation metrics can be used when restraints are applied in refinement
- Additional validation metrics for the model w.r.t. the data are needed
- We do not have cross-validation metrics for the model/data

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PHENIX Testers & Users

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